
MP4: Path Planning

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Overview

- Demo due 4/29/2021, Report due 4/30/2021
- 3 Written Questions, 4 Implementation Questions
- Written Questions:
 - A* Search
 - Probabilistic Road Maps
 - Value Iteration
- Implementation Questions
 - A* Planner v.s. Hybrid A* Planner
 - Design Choices
 - Video
 - Demo

Module Architecture

- **a_star.py**: You need to implement A*
- **hybrid_a_star.py**: You need to implement Hybrid A*
- **controller.py**: Dubin's Car Controller
- **mp4.py**: Main Function/ Wrapper
- **reset.py**: Resets Car Position (You need to reset to various different positions in this MP!)

A* Planner

- Keep track of both the cost of the partial path to get to a vertex $g(v)$ and the heuristic function estimating the cost to reach the goal from a vertex $h(v)$
- Choose a “ranking” function to be the sum of the two costs: $f(v) = g(v) + h(v)$
- **$g(v)$** : cost-to-arrive (from the start to v)
- **$h(v)$** : cost-to-go estimate (from v to the goal)
- **$f(v)$** : estimated cost of the path (from the start to v and then to the goal)

A* Planner

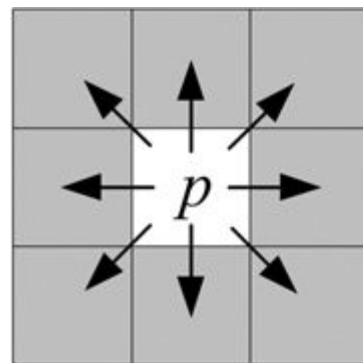
```
 $Q$   $\leftarrow$   $\langle start \rangle$  // initialize queue with start
while  $Q \neq \emptyset$ :
    pick (and remove) the path  $P$  with the lowest estimated cost ( $f(P) = g(P) + h(head(P))$ ) from  $Q$ 
    if  $head(P) = x_{goal}$  then return  $P$  // Reached the goal
    for each vertex  $v$  such that  $(head(P), v) \in E$ , do // for all neighbors
        add  $\langle v, P \rangle$  to  $Q$  // Add expanded paths
Return FAILURE // nothing left to consider
```

Heuristic

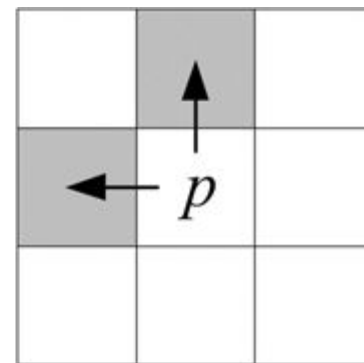
- Admissible heuristic: $h(v) \leq h^*(v)$
- $h^*(v)$: The actual cost from node to goal
- $h(v)$: Needs to be at most $h^*(v)$ to guarantee optimality
- But it doesn't mean $h(v)$ should be as small as possible!
 - When $h = 0$, A^* is equivalent to UCS
 - $h(v)$ should be as close to $h^*(v)$ as possible (Review partial order and domination)
- Consistent heuristic: $h(u) \leq w(u, v) + h(v)$
 - Satisfies triangle inequality
 - $f(v) = g(v) + h(v)$ is non-decreasing along paths
 - No need to compare costs or revisit expanded nodes

Euclidean distance

- Admissible?
- Consistent?
- Can you think about a better heuristic?
- Does it make sense to assign same edge weights/lengths to all neighbors?



(a)



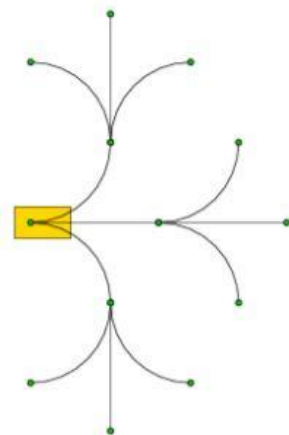
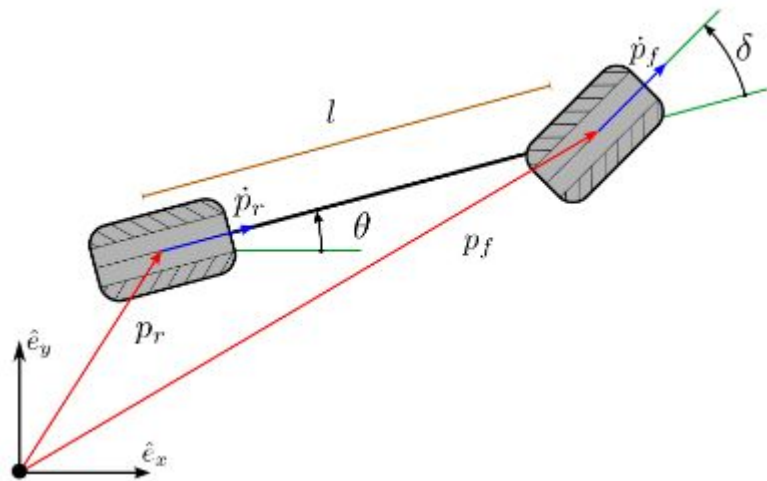
(b)

Nodes and Heap/ Priority Queue

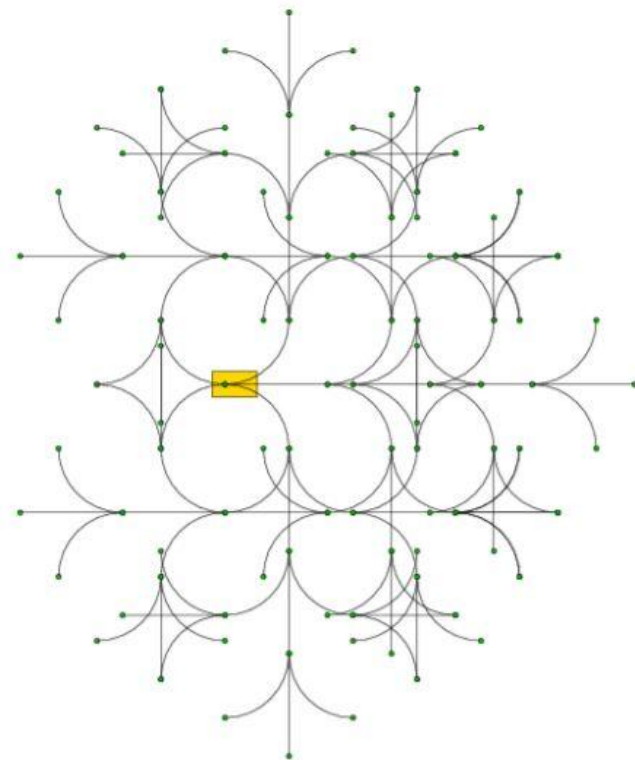
- A* node
 - Cost-to-arrive g
 - Estimated cost of the path: $f = g + h$ (heuristic to goal)
 - Position state: (x, y)
 - You can store path here also. Just need the ability to backtrack.
- Does popping smallest element sound familiar?
 - Heap (Python `heapq`)
- How do you construct nodes to be used in heap?
 - Easiest: Tuple with the key as the first element (f)
 - Cleaner: `__lt__` comparator in a class

Dubin's Car

- $x_{\text{new}} = x + v \cos(\theta)$
- $y_{\text{new}} = y + v \sin(\theta)$
- $\theta_{\text{new}} = \theta + v \tan(\delta) / l$



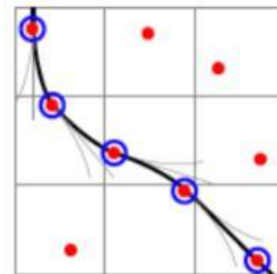
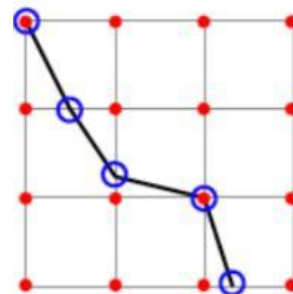
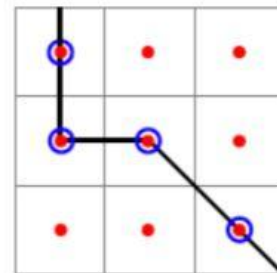
Two stages



Four stages

Hybrid A* Planner

- Problem with A*: Not good with continuous state space in real world
- Discrete path may not be executable by the vehicle dynamics
- Solution: Use representative continuous state on top of discrete nodes
- Hybrid A* Node
 - Cost-to-arrive g
 - Estimated cost of the path: $f = g + h$ (heuristic to goal)
 - Discrete position state: (x, y, θ)
 - Continuous position state: (x_c, y_c, θ_c)
 - Path or other information for backtracking



Transition and Discretization

- Say we start from a node with discrete state (x, y, θ) and continuous state (x_c, y_c, θ_c)
- We apply a control $u = (v, \delta)$ to (x_c, y_c, θ_c) from all the possible actions
- Now we get a continuous state (x_c', y_c', θ_c')
- We discretize (x_c', y_c', θ_c') to (x', y', θ') by rounding (or you can define your own resolution)
- (x', y', θ') is now the discrete state of your new node
- Cost g and h and path are still computed with continuous state
- Discrete state checks whether you've explored similar states (or goal)
- $(4.1, 5.9, 34.1^\circ)$ is the same as $(3.72, 6.22, 33.8^\circ)$ in terms of if you have visited it before or not

Demo

- The TA will pick a few test cases from the lab manual.
- Students need to show their A* and Hybrid A* planners
 - Finish planning within reasonable amount of time
 - A* planner needs to be optimal
 - Hybrid A* planner needs to have reasonably good performances

Questions?

- Again, start early