

# DEMO-Net: Degree-specific Graph Neural Networks for Node and Graph Classification



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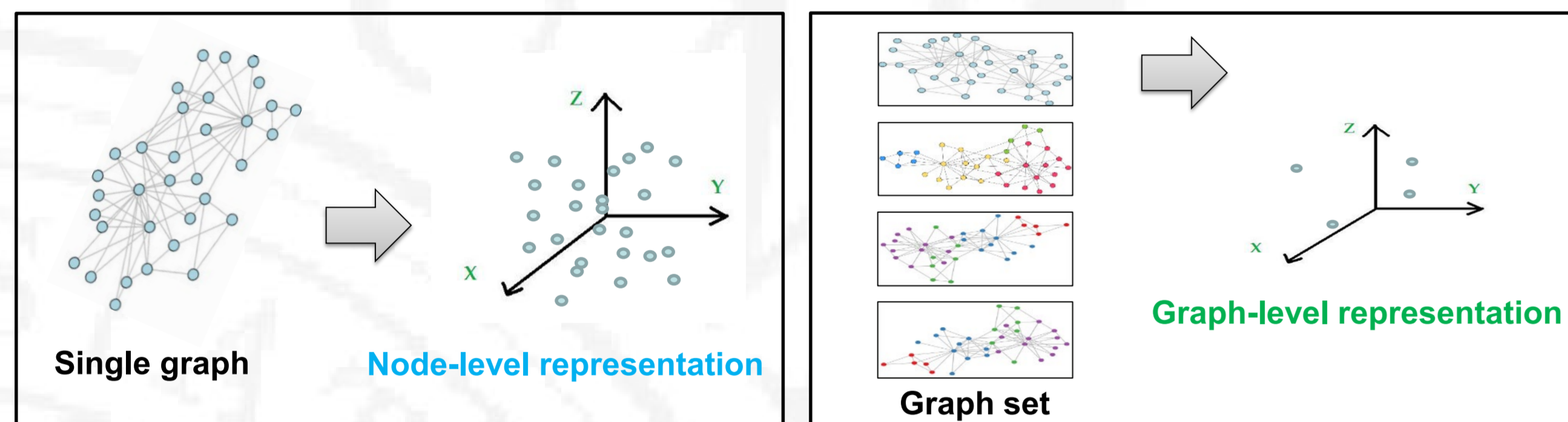
## Target Problems:

### Node-level representation learning

- Application: In a transaction network, the fraudulent users can be detected using the node (user) representation.

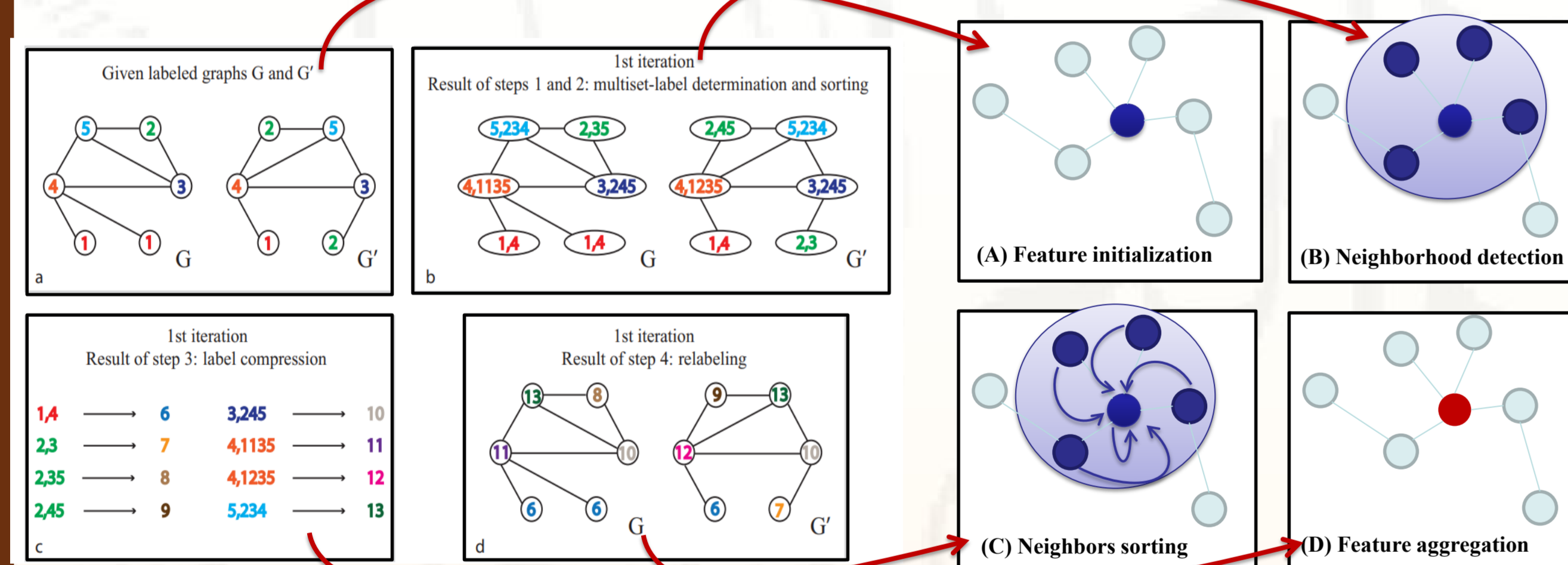
### Graph-level representation learning

- Application: In chemoinformatics, the toxic molecules (represented as graphs) can be classified using the graph (molecule) representation.



## Motivation:

- Graph convolution in graph neural networks has the similar steps as Weisfeiler-Lehman graph kernel.



Weisfeiler-Lehman graph kernel

Graph convolution operation

### Three properties on graph convolution:



## Proposed Framework:

### Multi-task graph convolution:

- Intuition: nodes with the identical degree value would share the same graph convolution function.
- Feature update:

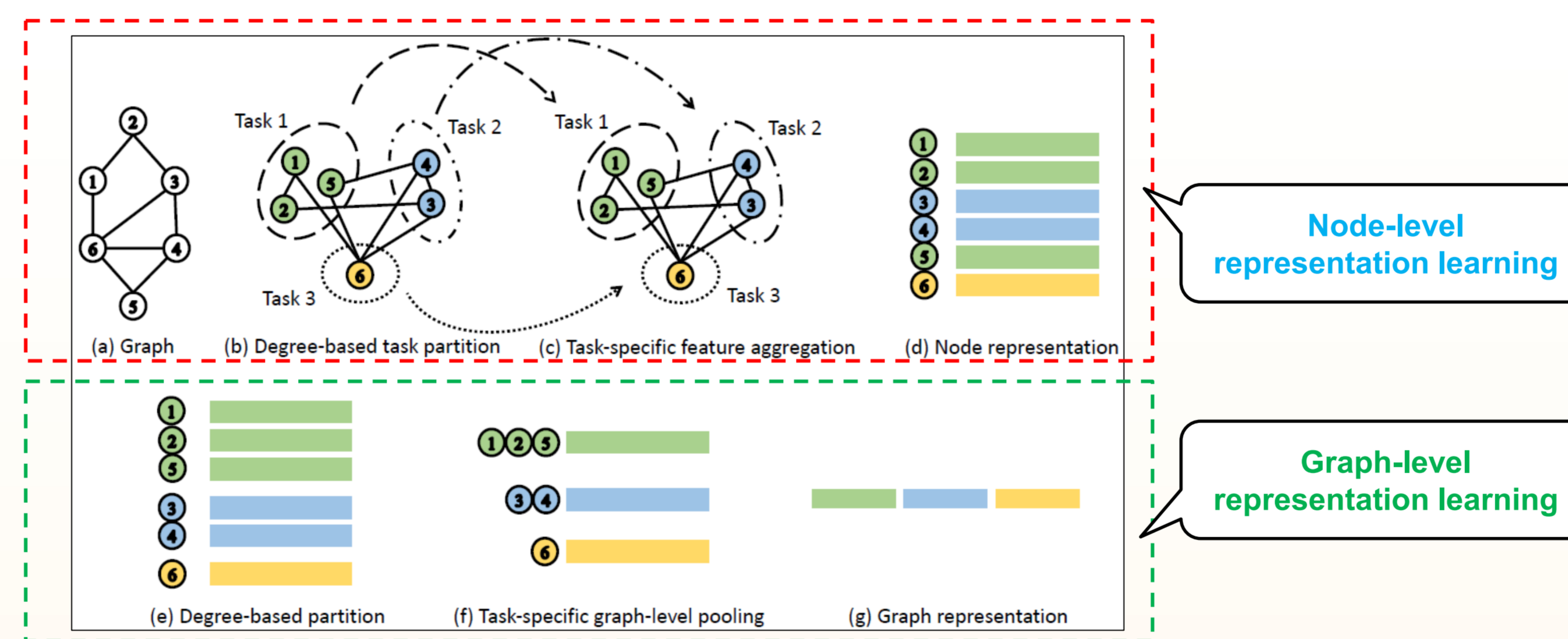
$$h_v^k = f_s(h_v^{k-1}) \circ f_{deg(v)}(\{h_u^{k-1} | u \in N(v)\}) = \sigma(W_0^k h_v^{k-1}) \circ f_{deg(v)}(h_{N(v)}^{k-1})$$

Multi-task convolution

Feature hashing:  $f_{deg(v)}(h_{N(v)}^{k-1}) = \sigma\left(\sum_{u \in N(v)} W^k (\phi_g(h_u^{k-1}) + \phi_{deg(v)}(h_u^{k-1}))\right)$

Weight sharing:  $f_{deg(v)}(h_{N(v)}^{k-1}) = \sigma\left(\sum_{u \in N(v)} (W_g^k + W_{deg(v)}^k) h_u^{k-1}\right)$

### DEMO-Net framework:



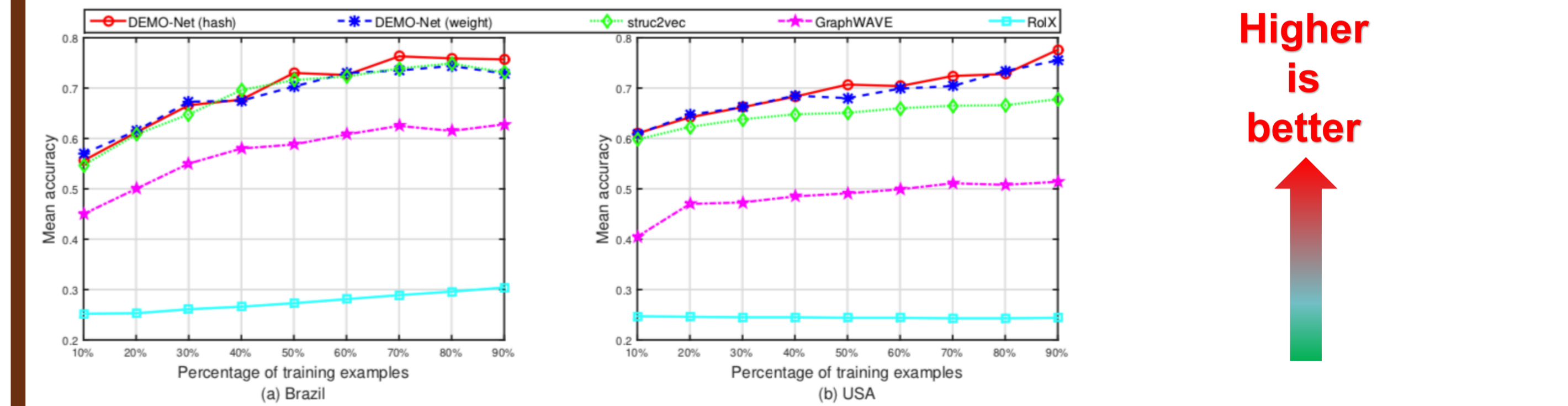
## Theoretical Analysis:

- (Existence Theorem) There exist the functions  $f_s$  and  $\{f_{deg} | deg \in degree(G)\}$  so that for any pair of subtrees, the composite function  $f_s \circ f_{deg}$  could map them to different feature vectors if they are not structurally identical.
- (Graph Kernel Space) The learned graph-level representation lies in a Reproducing Kernel Hilbert Space (RKHS) induced by a degree-specific Weisfeiler-Lehman graph kernel.

## Experimental Results:

### Node classification:

	Social networks				Air-traffic networks		
	Facebook	Wiki-Vote	BlogCatalog	Flickr	Brazil	Europe	USA
GraphSAGE [5]	0.389 ± 0.019	0.245 ± 0.000	0.828 ± 0.007	0.641 ± 0.006	0.404 ± 0.035	0.272 ± 0.022	0.316 ± 0.022
GCN [9]	0.575 ± 0.013	0.329 ± 0.029	0.720 ± 0.013	0.546 ± 0.019	0.432 ± 0.064	0.371 ± 0.046	0.432 ± 0.022
GCN_cheby [9]	0.646 ± 0.012	0.495 ± 0.016	0.686 ± 0.037	0.479 ± 0.023	0.516 ± 0.070	0.460 ± 0.038	0.526 ± 0.045
Union [12]	0.600 ± 0.000	0.463 ± 0.000	0.730 ± 0.000	0.566 ± 0.000	0.466 ± 0.006	0.418 ± 0.002	0.582 ± 0.000
Intersection [12]	0.598 ± 0.000	0.462 ± 0.000	0.725 ± 0.000	0.557 ± 0.000	0.459 ± 0.003	0.443 ± 0.002	0.573 ± 0.000
GAT [18]	0.570 ± 0.036	0.594 ± 0.070	0.663 ± 0.000	0.359 ± 0.000	0.382 ± 0.126	0.424 ± 0.073	0.585 ± 0.021
DEMO-Net(hash)	0.887 ± 0.020	0.997 ± 0.000	0.849 ± 0.006	<b>0.678 ± 0.010</b>	<b>0.614 ± 0.069</b>	<b>0.479 ± 0.064</b>	<b>0.659 ± 0.020</b>
DEMO-Net(weight)	<b>0.919 ± 0.003</b>	<b>0.998 ± 0.000</b>	<b>0.849 ± 0.000</b>	0.656 ± 0.000	0.543 ± 0.034	0.459 ± 0.025	0.647 ± 0.021

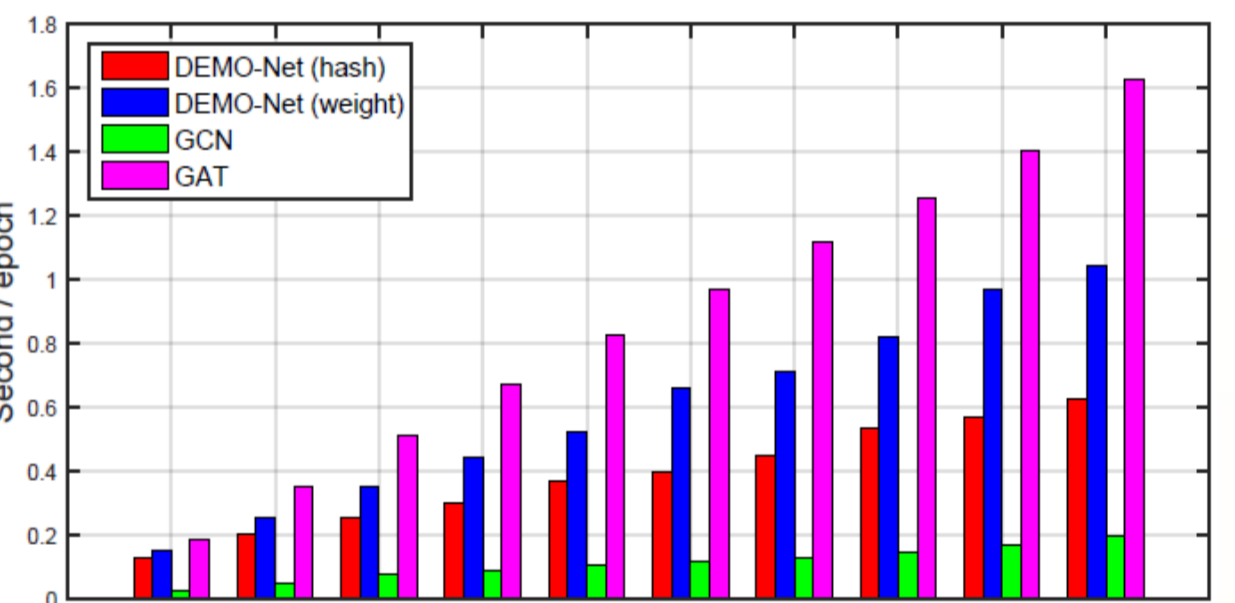


Higher is better

### Graph classification:

	MUTAG	PTC	PROTEINS	ENZYMES
DeepWL [23]	0.733	0.537	0.680	0.210
DCNN [1]	0.670	0.572	0.579	0.160
PATCHY-SAN [13]	0.795	0.568	0.714	0.170
DIFFPOOL [24]	0.663	0.251	<b>0.733</b>	0.184
DEMO-Net_m(hash)	0.760	<b>0.586</b>	0.617	0.236
DEMO-Net_m(weight)	0.798	0.550	0.616	0.251
DEMO-Net(hash)	0.771	0.563	0.705	0.251
DEMO-Net(weight)	<b>0.814</b>	0.572	0.708	<b>0.272</b>

### Efficiency:



## Conclusion:

- Association of three key properties for graph convolution with Weisfeiler-Lehman isomorphism test.
- A novel degree-specific graph neural network model (DEMO-Net) for encoding the subtree structures from graphs.
- Extensive results demonstrating the proposed DEMO-Net method.

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