

## TECHNICAL ADVANCE

# Gap filling strategies and error in estimating annual soil respiration

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## Abstract

Soil respiration ( $R_{\text{soil}}$ ) is one of the largest  $\text{CO}_2$  fluxes in the global carbon (C) cycle. Estimation of annual  $R_{\text{soil}}$  requires extrapolation of survey measurements or gap filling of automated records to produce a complete time series. Although many gap filling methodologies have been employed, there is no standardized procedure for producing defensible estimates of annual  $R_{\text{soil}}$ . Here, we test the reliability of nine different gap filling techniques by inserting artificial gaps into 20 automated  $R_{\text{soil}}$  records and comparing gap filling  $R_{\text{soil}}$  estimates of each technique to measured values. We show that although the most commonly used techniques do not, on average, produce large systematic biases, gap filling accuracy may be significantly improved through application of the most reliable methods. All methods performed best at lower gap fractions and had relatively high, systematic errors for simulated survey measurements. Overall, the most accurate technique estimated  $R_{\text{soil}}$  based on the soil temperature dependence of  $R_{\text{soil}}$  by assuming constant temperature sensitivity and linearly interpolating reference respiration ( $R_{\text{soil}}$  at 10 °C) across gaps. The linear interpolation method was the second best-performing method. In contrast, estimating  $R_{\text{soil}}$  based on a single annual  $R_{\text{soil}} - T_{\text{soil}}$  relationship, which is currently the most commonly used technique, was among the most poorly-performing methods. Thus, our analysis demonstrates that gap filling accuracy may be improved substantially without sacrificing computational simplicity. Improved and standardized techniques for estimation of annual  $R_{\text{soil}}$  will be valuable for understanding the role of  $R_{\text{soil}}$  in the global C cycle.

**Keywords:** calculation error, carbon cycle, measurement, temporal extrapolation

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## Introduction

Soil respiration ( $R_{\text{soil}}$ ) is one of the largest  $\text{CO}_2$  fluxes in the global carbon (C) cycle, contributing up to 80 Pg C to the atmosphere annually (Schlesinger, 1977; Raich *et al.*, 2002), and plays an important role in regulating the feedbacks between terrestrial ecosystems and the atmosphere (Raich *et al.*, 2002; Field *et al.*, 2007). Quantifying the contribution of  $R_{\text{soil}}$  to the global C cycle requires estimates of total annual  $R_{\text{soil}}$ . However, the large temporal variability in  $R_{\text{soil}}$  rates presents a methodological challenge to obtaining reliable annual sums.

Measurements of  $R_{\text{soil}}$  may be made using either manual or automated systems (reviewed in Savage &

Davidson, 2003; Savage *et al.*, 2008). Regardless of the methodology used, continuous year-long data records appropriate for constructing annual  $R_{\text{soil}}$  sums are generally not obtained. Manual systems are limited to low sampling frequency, yielding a record that is mostly gap (>99% of half hour periods throughout a year for biweekly sampling). Measurements typically are made at weekly to monthly intervals for the growing season or an entire year, and over a specific period of the day believed to be representative of the daily  $R_{\text{soil}}$  flux (typically during daytime hours; e.g. Davidson *et al.*, 1998; Savage & Davidson, 2003). Thus, gap occurrence in manual  $R_{\text{soil}}$  datasets is nonrandom, with data existing for defined times – generally at approximately the same time of day and with a potentially strong bias toward favorable sampling conditions (e.g. nonstormy days). As of yet, there is no consensus as to the best methodology for extrapolation of these low-frequency measurements to produce annual  $R_{\text{soil}}$  estimates.

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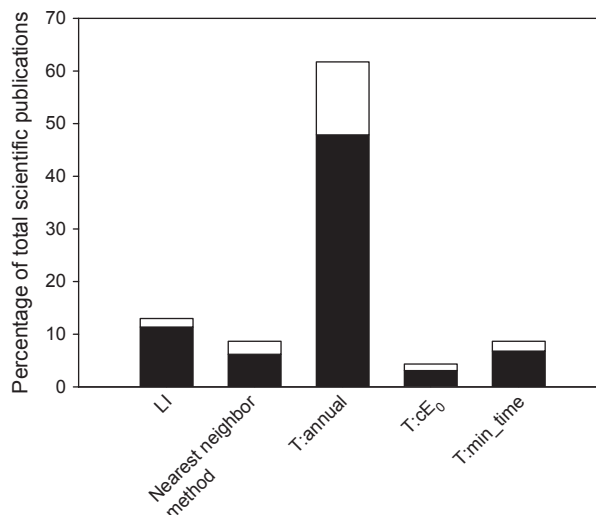
Automated systems are designed to sample  $R_{\text{soil}}$  continuously over long periods of time, often with the purpose of obtaining annual estimates. Measurements typically occur at least once per hour throughout the day. Although these systems can in theory provide a continuous data record for an entire year, the data records usually contain gaps (e.g. Wu *et al.*, 2010). Gaps occur for a variety of reasons, including unrepresentative conditions (e.g. plant growth inside a  $R_{\text{soil}}$  collar), instrument damage or failure, low quality of the data, and intentional shutdown because of unfavorable conditions (e.g. snow). Data gaps in automated  $R_{\text{soil}}$  records are semi random, occurring at any time of the day or year, but are more likely to occur under certain conditions (e.g. winter). Gaps vary in length from less than an hour to multiple weeks. As with automated systems, there is no consensus regarding the best methodology for gap filling automated  $R_{\text{soil}}$  records.

A variety of methods have been employed to gap fill  $R_{\text{soil}}$  records to produce annual estimates (Fig. 1), including simple algorithms (e.g. linear interpolation) or by prediction of missing values based on the relationship of  $R_{\text{soil}}$  to known variables (e.g. soil temperature). The linear interpolation method is commonly used (Fig. 1; e.g. Savage & Davidson, 2003). Implicit in this method are the assumptions that (1)  $R_{\text{soil}}$  changes at a constant rate between one measured record and the next, and (2) measurements are timed so as to characterize all critical points in the time series. Both these assumptions are violated by real  $R_{\text{soil}}$  time series because measurements do not typically characterize diurnal variation and because  $R_{\text{soil}}$  varies nonlinearly through time. However, if measurements are timed so as to characterize average daily  $R_{\text{soil}}$ , this method can be the most practical means of estimating annual  $R_{\text{soil}}$  when soil micrometeorology data are unavailable. Other simple algorithms, such as cubic interpolation or monthly average methods, may also be viable gap filling methods.

When continuous records of variables that drive  $R_{\text{soil}}$  are available, missing values may be predicted based upon these variables. The most frequently used variable is soil temperature, which is generally a good predictor of  $R_{\text{soil}}$  (Raich & Schlesinger, 1992; Raich *et al.*, 2002; but see Davidson *et al.*, 2006; Gomez-Casanovas *et al.*, 2012). The relationship between temperature and  $R_{\text{soil}}$  has been described using a variety of exponential functions; one of the most accurate and widely used functions is that proposed by Lloyd & Taylor (1994):

$$R_{\text{soil}}(T) = R_{\text{ref}} e^{E_0 \left( \frac{1}{T_{\text{ref}} - T_0} - \frac{1}{T - T_0} \right)} \quad (1)$$

Here,  $R_{\text{ref}}$  is respiration at a reference temperature ( $T_{\text{ref}}$ ; often 10 °C),  $E_0$  is a fitted parameter characterizing the



**Fig. 1** Published strategies used to gap fill  $R_{\text{soil}}$  records. A literature search was conducted using Science Citation Index Expanded database from ISI Web of Knowledge, Web of Science with annual sum of  $R_{\text{soil}}$  rates obtained using either manual (closed bar) or automated (open bar) systems with no restriction on date of publication. A total of 177 scientific publications were found that met these criteria, and these publications reported 196 values of annual  $R_{\text{soil}}$  sums (Appendix S1). Methods are as described in Table 1, with the caveat that the temperature-dependence models (T : annual, T : cE<sub>0</sub>, T : min\_time) are more broadly defined to include fits based on Van't Hoff, Arrhenius, or the Lloyd and Taylor respiration functions (Lloyd & Taylor, 1994). Studies are counted as T : min\_time if  $E_0$  (or  $Q_{10}$ ) (temperature sensitivity of  $R_{\text{soil}}$ ) and  $R_{\text{ref}}$  (temperature-standardized respiration rate) were calculated by fitting more than a single relationship between  $R_{\text{soil}}$  and soil temperature for the year (e.g. growing season and nongrowing season; Ruehr *et al.*, 2010). From a total of 177 scientific publications, 5% of the soil temperature methods assumed an interaction between soil temperature and moisture, whereas 13% of these methods assumed no interaction between these two variables.

temperature sensitivity (Arrhenius, 1889), and  $T_0$  is the lower temperature limit for  $R_{\text{soil}}$ . This model has two fitted parameters that may vary substantially over the course of a year,  $R_{\text{ref}}$  and  $E_0$ .  $R_{\text{ref}}$  is a temperature-standardized respiration rate which may be influenced by many variables including root biomass, the size and composition of the microbial community, belowground carbon allocation by plants, the quantity and quality of C compounds in the soil, and soil moisture.  $E_0$  theoretically characterizes the inherent temperature sensitivity of aerobic respiration; however, the apparent value of  $E_0$  will be altered if  $R_{\text{ref}}$  varies at the time scale over which the model is applied (Curiel-Yuste *et al.*, 2004; Davidson *et al.*, 2006; Sampson *et al.*, 2007; Anderson-Teixeira *et al.*, 2008). The most commonly used method of extrapolating incomplete  $R_{\text{soil}}$  records to yield an annual estimate is predicting missing values based on a fitting of Eqn 1 (or a

similar function) to the entire annual dataset (Fig. 1; e.g. Irvine & Law, 2002). Implicit in this approach are the assumptions that  $E_0$  and  $R_{\text{ref}}$  both are constant over the year. However,  $E_0$  and  $R_{\text{ref}}$  can vary seasonally (Curiel-Yuste *et al.*, 2003; Janssens & Pilegaard, 2003; Sampson *et al.*, 2007; Chen *et al.*, 2010), implying that better models may be obtained by allowing one or both parameters to vary throughout the year. Relatively few studies have employed gap filling techniques that allow  $E_0$  or  $R_{\text{ref}}$  to vary over the year (Fig. 1; e.g. Anderson-Teixeira *et al.*, 2013; Drake *et al.*, 2011).

Models predicting  $R_{\text{soil}}$  may be further improved by including soil moisture and correlates of primary productivity (e.g. leaf area index; Reichstein *et al.*, 2003). Including soil moisture in models to gap fill  $R_{\text{soil}}$  datasets is complex (Reichstein & Beer, 2008) because soil water status can affect several physiological parameters such as enzyme activities, or the turnover of roots and soil microorganisms. In addition, soil water status can affect gas and substrate diffusion thereby affecting substrate availability (Rodrigo *et al.*, 1997). Soil moisture

and temperature often interact;  $E_0$  generally decreases with decreases in soil moisture (Reichstein *et al.*, 2002a, b; Janssens & Pilegaard, 2003). The interactive effects of soil temperature and moisture may be described using the following equation (Reichstein *et al.*, 2003):

$$R_{\text{soil}} = R_{\text{ref}} \cdot e^{E_0(\text{RSWC}) \cdot \left( \frac{1}{T_{\text{ref}} - T_0} - \frac{1}{T_{\text{soil}} - T_0} \right)} \cdot \frac{\text{RSWC}}{\text{RSWC}_{1/2} + \text{RSWC}} \quad (2)$$

Here, RSWC is relative soil water content ( $\text{RSWC} = \text{SWC}/\text{SWC}_{\text{FC}}$ ), where SWC is soil water content in  $\text{m}^3 \text{m}^{-3}$ ,  $\text{SWC}_{\text{FC}}$  is soil water content at field capacity and  $\text{RSWC}_{1/2}$  is the RSWC where  $R_{\text{soil}}$  is half its maximal value (at a given temperature).  $E_0$  is assumed to vary linearly with RSWC ( $E_0(\text{RSWC}) = a + b \cdot \text{RSWC}$ , where  $a$  and  $b$  are fitted parameters). Although gap filling methods using both soil temperature and moisture are rare (Reichstein *et al.*, 2003), models incorporating temperature-moisture interactions may yield improvements for predicting  $R_{\text{soil}}$ .

**Table 1** Gap filling strategies evaluated in this study. Full methodological details are presented in Appendix S1

Method	Data required	Description
<b>Simple Algorithm Methods</b>		
Linear Interpolation (LI)	$R_{\text{soil}}$	Missing $R_{\text{soil}}$ rates extrapolated by linear interpolation to the entire year
Cubic Interpolation (CI)		Missing $R_{\text{soil}}$ rates extrapolated by cubic interpolation to the entire year
Monthly Average (MA)		For gap time frames <30 days, missing $R_{\text{soil}}$ values replaced by the average of $R_{\text{soil}}$ data for the current month
<b>Soil Temperature-Dependence Methods</b>		
Temperature dependence, fit annually (T : annual)	$R_{\text{soil}}, T_{\text{soil}}$	$E_0$ and $R_{\text{ref}}$ calculated by fitting a single relationship between $R_{\text{soil}}$ and temperature for the entire year
Constant temperature sensitivity, varying $R_{\text{ref}}$ (T : $cE_0$ )		$E_0$ assumed to be constant for the entire year ( $308.56 \text{ K}^{-1}$ ); $R_{\text{ref}}$ calculated at each time frame for which $R_{\text{soil}}$ data was available and then extrapolated to the entire year using a linear interpolation
Temperature dependence, fit over minimum time frame (T : min_time)		$E_0$ and $R_{\text{ref}}$ fitted using the shortest possible time for characterizing the relationship between $R_{\text{soil}}$ and soil temperature for which sufficient data are available. Defaults to linear interpolation when fitting fails or is unrealistic
<b>Soil Temperature- and Moisture-Dependence Methods</b>		
Temperature $\times$ moisture dependence, fit annually (TxSWC : annual)	$R_{\text{soil}}, T_{\text{soil}}, \text{RSWC}$	$E_0(\text{RSWC})$ and $R_{\text{ref}}$ calculated by fitting a single relationship between $R_{\text{soil}}$ , soil temperature and moisture (Eqn 2) for the entire year
Constant temperature sensitivity, $R_{\text{ref}}$ moisture-dependent (T+SWC : $cE_0$ )		$E_0$ assumed to be constant for the entire year ( $308.56 \text{ K}^{-1}$ ); $R_{\text{ref}}$ calculated by assuming a linear dependency of $R_{\text{ref}}$ on the relative water content (RSWC)
Temperature $\times$ moisture dependence, fit over minimum time frame (TxSWC : min_time)		$E_0(\text{RSWC})$ and $R_{\text{ref}}$ calculated using the shortest possible time for characterizing the relationship between $R_{\text{soil}}$ , soil temperature and moisture (Eqn 2) for which sufficient data are available. Defaults to linear interpolation when fitting fails or is unrealistic

The reliability of various strategies for filling gaps in  $R_{\text{soil}}$  records has not been assessed (Vargas *et al.*, 2010). In this study, we evaluate the performance of different gap filling methods (Table 1) using measured records with varying gap fractions. Specifically, we evaluate the performance of these different gap filling methods by analyzing the errors introduced when filling artificial gaps in automated  $R_{\text{soil}}$  datasets obtained over 3 years for various ecosystem types. Introduced gaps ranged from none to >99% gap. In addition, we analyzed how the timing of survey measurements (>99% gap) affected gap filling performance, considering two time frames for measurement (9:00 hours–17:00 hours and 9:00 hours–12:00 hours) and two portions of the year (entire year and growing season only). We use our results to provide guidance as to which gap filling methods should be used to provide accurate annual  $R_{\text{soil}}$  estimates for both automated and manual  $R_{\text{soil}}$  systems.

## Materials and methods

### Study site

High-frequency data for this analysis were collected from research plots at the University of Illinois Energy Farm in Urbana, IL (40°3'46.209"N, 88°11'46.0212"W, ca. 220 m above sea level). Average mean monthly (1979–2009) air temperature was 11.1 °C while the mean accumulated rainfall was 1042 mm (Illinois State Water Survey Historic Climate Data). For the 3 years used in this study (2009, 2010 and 2011), annual mean temperature was 10.4, 11.3, and 11.6 °C, respectively, according to measurements from a weather station located ca. 5 km away at the University of Illinois-Willard Airport. Cumulative rainfall from the same weather station for these 3 years was 1147, 898, and 921 mm, respectively. The study area is flat and soils belong to silt loam Flanagan soil series with small contributions of Drummer soils. The experimental plots at the Energy Farm consisted of four 3.8-ha plots, each planted with miscanthus (*Miscanthus × giganteus*), switchgrass (*Panicum virgatum* L), a mix of native prairie species (see Zeri *et al.*, 2011 for species list), or a corn-corn-soybean rotation. Prior to this experiment, these plots were cultivated with annual arable crops for over 100 years. Land conversion into the experimental plots occurred in spring 2008. Details about crop management after land conversion at this site can be found in Zeri *et al.* (2011).

### $R_{\text{soil}}$ , temperature and moisture measurements

$R_{\text{soil}}$  was measured continuously from January 2009 to December 2011 in each experimental plot with an automated system consisting of an infrared gas analyzer (LI-8100-101; Licor, Inc., Lincoln, NE, USA) connected to a multiplexer (LI-8150; Licor, Inc.) controlling four automated 20-cm diameter chambers (LI-8011; Licor, Inc.). Each chamber was located ca. 15 m from the center of the plot. Each chamber closed on a PVC collar

permanently inserted ca. 2–5 cm into the soil.  $R_{\text{soil}}$  fluxes were measured every half hour providing a total of 48 annual  $R_{\text{soil}}$  records (i.e. 4  $R_{\text{soil}}$  records per plot for 3 years). Quality control of the data consisted on deleting  $R_{\text{soil}}$  values associated with equipment malfunction (e.g. chamber close failures, pump failures, damaged air hoses) and anomalous values (e.g. from plant growth within the chamber space). Only those  $R_{\text{soil}}$  records with less than 50% of data missing were used in this study, yielding a total of 20  $R_{\text{soil}}$  records. On average, 33% of the  $R_{\text{soil}}$  data was missing for 2009, 2010, and 2011  $R_{\text{soil}}$  datasets. The 20  $R_{\text{soil}}$  records were evenly distributed among the four ecosystems. Soil temperature at 5 cm and moisture at 10-cm depth were also measured continuously every half-hour within each plot. Quality control of the data consisted on the removal of out-of-range values ( $\pm 3.5$  standard deviations from the mean).

### Artificial gap creation and filling

To investigate the performance of each gap filling strategy (Table 1), artificial gaps were created in the 20 records of annual  $R_{\text{soil}}$  using code written in Matlab® v. 7.8.0. As  $R_{\text{soil}}$  records already contained real gaps, artificial gaps were only created in periods of existing data. This allowed for the analysis of the performance of each method when existing and predicted  $R_{\text{soil}}$  data were compared. Artificial gaps were introduced at 12 gap fractions (i.e. length of gap relative to the existing half hour  $R_{\text{soil}}$  rates): 0%, 5%, 15%, 25%, 35%, 45%, 55%, 65%, 75%, 85%, 95%, and >99% of the existing data. The highest gap scenario (>99% gap) mimicked a typical survey measurement scheme, with bimonthly measurements made between 9:00 hours and 17:00 hours at random dates in the first and second halves of each month.

Because gaps in automated  $R_{\text{soil}}$  records are nonrandomly distributed, occurring in clusters rather than as half-hour gaps randomly distributed throughout the record, artificial gaps were introduced to simulate the distribution of real gaps. This was critical because the performance of each method depends on the randomness of the gap distribution (Falge *et al.*, 2001). In our 48 automated  $R_{\text{soil}}$  records, less than 10% of the gaps occurred at a frequency of single half-hours, 60% of the gaps occurred at time frames between half-hours and 30 days, and 40% occurred at >30 days. This frequency distribution of gaps in  $R_{\text{soil}}$  records was mimicked when creating artificial gaps. As gaps introduced in this manner approached but did not exactly meet the target gap fractions, random half-hour gaps were inserted to make up the difference necessary to achieve the exact introduced gap fraction target.

For each  $R_{\text{soil}}$  chamber record, the artificial gap construction algorithm was permuted 100 times at each gap fraction, giving a total of 2000 records containing artificial gaps for each gap fraction. Artificial gaps were filled using each of the nine gap filling strategies (Table 1; detailed in Appendix S2). With 100 permutations of artificial gap creation, the standard error of the predicted annual  $R_{\text{soil}}$  sum obtained from each method at each gap fraction was accurate to within 10%.

In addition to the analysis of gap filling performance as a function of gap fraction, we also compared performance of gap

filling method for four different simulated survey respiration schemes: (1) bimonthly measurements over the entire year between 9:00 hours and 17:00 hours (same as in the above analysis), (2) bimonthly measurements over the entire year between 9:00 hours and 12:00 hours – a time frame that has been recommended as representative of the average daily  $R_{\text{soil}}$  (Davidson *et al.*, 1998), (3) bimonthly measurements over the growing season (April–October) between 9:00 hours and 17:00 hours, and (4) bimonthly measurements over the growing season (April–October) between 9:00 hours and 12:00 hours. Gaps were constructed and filled as described above, with the exception that the T : min\_time and TxSWC : min\_time methods (detailed in Appendix S2) were not evaluated, as these are theoretically identical to their annual fitting counterparts (T : annual and TxSWC : annual, respectively) or to LI (when curve fitting fails) at the highest gap fraction.

### Statistical analysis and annual $R_{\text{soil}}$ sum

For statistical purposes, the performance of each method at each gap fraction was evaluated by comparing the filled  $R_{\text{soil}}$  data with the observed values. The coefficient of determination ( $R^2$ ) and the root mean square error (RMSE) between the observed and predicted  $R_{\text{soil}}$  values was obtained. In addition, the potential bias error (BE), annual  $R_{\text{soil}}$  sum ( $\Sigma R_{\text{soil}}$ ), and the ratio between the predicted and observed  $\Sigma R_{\text{soil}}$  was calculated for each gap fraction for each gap filling method. The coefficient of determination ( $R^2$ ), RSME, and BE between the predicted (p) and the observed (o)  $R_{\text{soil}}$  values at any given time were calculated as in Moffat *et al.* (2007).

The  $\Sigma R_{\text{soil}}$  was calculated using the following equation:

$$\sum R_{\text{soil}} = \sum R_{\text{soil}} \cdot \Delta t \quad (3)$$

Here,  $R_{\text{soil}}$  is the  $R_{\text{soil}}$  rate at any given half-hour and  $\Delta t$  is the measurement time interval. In addition, the ratio between the predicted and observed  $\Sigma R_{\text{soil}}$  ( $\Sigma R_{\text{soil}}$  ratio) was calculated.

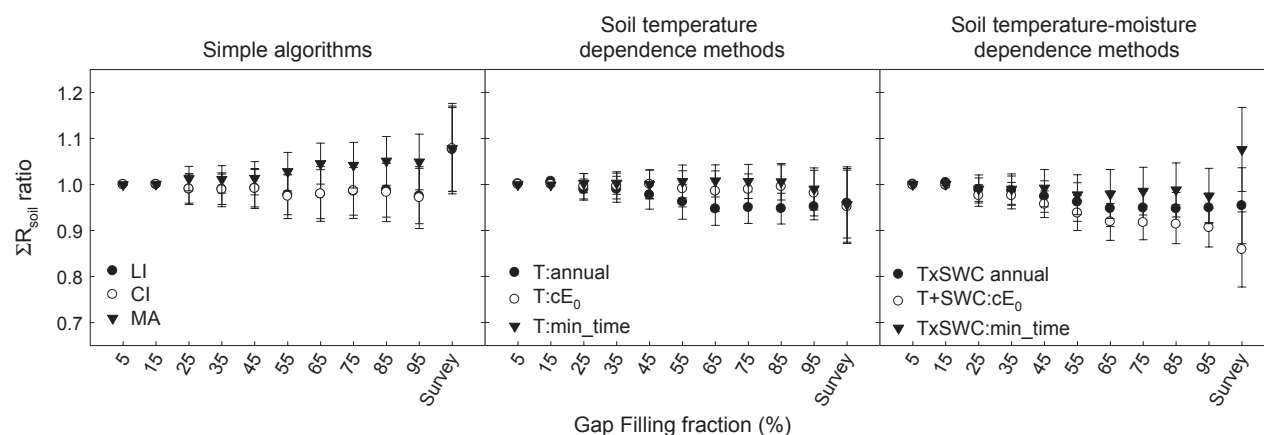
The performance of each gap filling strategy at each gap fraction was assessed with one-way analysis of variance (ANOVA) analysis. Gap filling strategy was set as a main factor, with years (2008, 2009, and 2011) and vegetation type (*Miscanthus*, switchgrass, perennial grass native, and a corn-corn-soy rotation) as covariates. To test their performance, the methods were ranked according to each of the statistical metrics (e.g.  $R^2$ , RSME, BE,  $\Sigma R_{\text{soil}}$  ratio) based on a multiple comparison test as in Moffat *et al.* (2007). These tests were implemented using Statgraphics Plus 5.0 (Statistical Graphics Corporation, Rockville, MD, USA).

The  $R^2$  and RSME tested for the accuracy of each model (in phase correlation, and magnitude and distribution of the individual errors, respectively), and BE and the  $\Sigma R_{\text{soil}}$  ratio indicate the bias induced in the estimated half-hour  $R_{\text{soil}}$  rates and  $\Sigma R_{\text{soil}}$ , respectively. For instance, a method with low  $R^2$  and a  $\Sigma R_{\text{soil}}$  ratio close to 1 would indicate that whereas the accuracy of the model is low, overestimates of half-hour  $R_{\text{soil}}$  values are being cancelled by underestimates, yielding reasonable estimates of  $\Sigma R_{\text{soil}}$ .

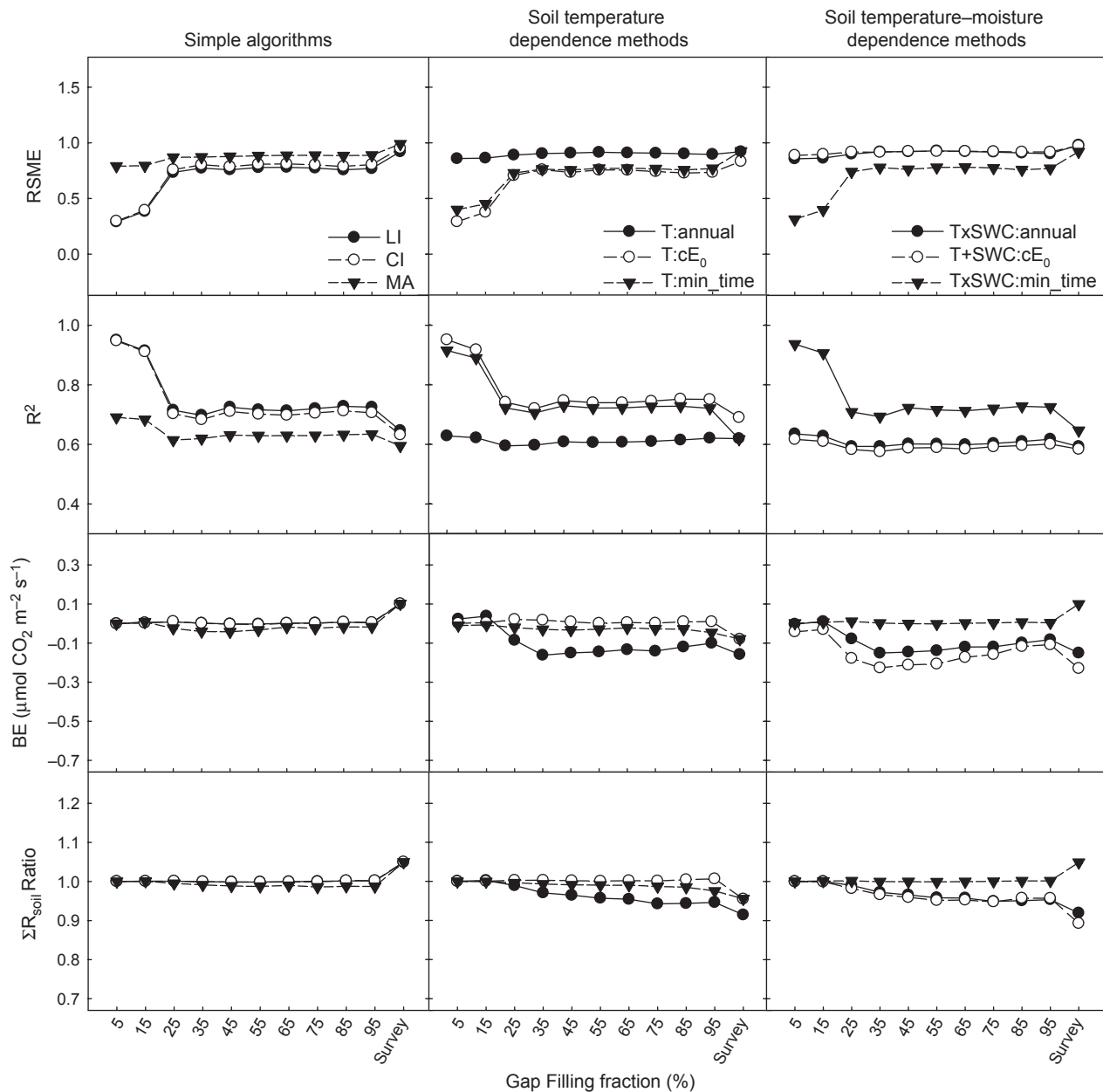
### Results

The ability of all gap filling models to accurately predict  $\Sigma R_{\text{soil}}$  decreased above 15% and the variability increased with increasing gap fraction (Fig. 2). Inaccuracy and variability in the gap filling methods increased substantially for the simulated survey record (>99% gap fraction) relative to 95% gap fraction. Each method either consistently under- or overestimated BE and the  $\Sigma R_{\text{soil}}$  ratio. The performance of the various gap filling methods (Table 1) varied across  $R_{\text{soil}}$  records and the overall performance of each method was assessed by comparing statistics across all records.

Averaged across 20  $R_{\text{soil}}$  records, permuted 100 times, RSME increased with increasing gap fraction (Fig. 3).



**Fig. 2** The performance of three contrasting gap filling methods in estimating  $\Sigma R_{\text{soil}}$  across a range of gap fractions. Values are means  $\pm$  standard deviation of the ratio of gap filled to real  $\Sigma R_{\text{soil}}$  ( $\Sigma R_{\text{soil}}$  ratio) for 100 artificial gap permutations of one record (switchgrass, 2009). Gap filling methods include the simple algorithms, soil temperature-dependence and soil temperature-moisture-dependence methods and are abbreviated as in Table 1.



**Fig. 3** Average performance of three contrasting gap filling methods across a range of gap fractions. Shown are means  $\pm$  standard error of RMSE,  $R^2$ , bias error (BE), and the ratio of gap filled to real  $\Sigma R_{soil}$  ( $\Sigma R_{soil}$  ratio) for 20 records run 100 times each. Standard error values are smaller than symbols used for means. These metrics represent the average performance of each method over 100 artificial gap permutations as opposed to the expected performance on any one gap scenario (Fig. 2). Gap filling methods include the simple algorithms, soil temperature-dependence and soil temperature-moisture-dependence methods, and are abbreviated as in Table 1.

The statistical comparison of the RSME at 95% confidence level allowed for the evaluation of each method's performance at each gap fraction (Fig. 3; Table 2). At all gap fractions, the soil temperature method with constant temperature sensitivity and varying  $R_{ref}$  (i.e. the T : cE<sub>0</sub> method) had the lowest RSME (Fig. 3; Table 2). In addition, the RSME for the T : min\_time method was the lowest at gap fractions between 25% and 65%

(Fig. 3; Table 2). In contrast, methods that filled gaps based upon a single temperature-dependence or temperature- and moisture-dependence function (i.e. T : annual, TxSWC : annual, and T+SWC : cE<sub>0</sub> methods) had the highest RSME at all gap fractions evaluated, and at > 99% gap fraction the MA method had the highest RSME (Fig. 3; Table 2). The MAE (data not shown) of the gap fractions from each gap filling

**Table 2** Methods performance at each gap fraction according to their RMSE (Root Mean Square Error),  $R^2$ , BE (Bias Error) and  $\Sigma R_{\text{soil}}$  ratio (ratio between predicted and observed  $\Sigma R_{\text{soil}}$ ). The 'best performance' refers to methods that ranked significantly better than the others (95% CI), whereas 'poorest performance' refers to methods that ranked lowest based on each statistical metric. For each gap fraction level, methods that performed consistently best or poorest across all performance metrics are in bold. The survey scheme used in this analysis was Annual: 0900 CST-1700 CST

Gap fraction (%)	Best performance				Poorest performance			
	RMSE	$R^2$	BE	$\Sigma R_{\text{soil}}$ ratio	RMSE	$R^2$	BE	$\Sigma R_{\text{soil}}$ ratio
5	<b>LI, CI, T : cE<sub>0</sub></b>	<b>LI, CI</b> T : cE <sub>0</sub>	<b>LI, CI</b> T : cE <sub>0</sub>	<b>LI, CI</b> T : cE <sub>0</sub>	T+SWC : cE <sub>0</sub>	T : annual T+SWC : cE <sub>0</sub>	T : annual	T : annual
15	<b>LI</b> T : cE <sub>0</sub>	<b>LI, CI</b> TxSWC : min_time	<b>LI, CI</b> T : cE <sub>0</sub>	<b>LI, CI</b> T : cE <sub>0</sub>	T+SWC : cE <sub>0</sub>	T : annual T+SWC : cE <sub>0</sub>	T : annual	T : annual
25	T : min_time <b>T : cE<sub>0</sub></b>	LI <b>T : cE<sub>0</sub></b>	LI, CI <b>T : cE<sub>0</sub></b>	LI, CI <b>T : cE<sub>0</sub></b>	<b>T+SWC : cE<sub>0</sub></b> TxSWC : annual	T : annual <b>T+SWC : cE<sub>0</sub></b> TxSWC : annual	<b>T+SWC : cE<sub>0</sub></b>	<b>T+SWC : cE<sub>0</sub></b>
35	T : min_time <b>T : cE<sub>0</sub></b>	LI <b>T : cE<sub>0</sub></b>	LI, CI <b>T : cE<sub>0</sub></b>	LI, CI <b>T : cE<sub>0</sub></b>	T : annual <b>T+SWC : cE<sub>0</sub></b>	T : annual <b>T+SWC : cE<sub>0</sub></b>	<b>T+SWC : cE<sub>0</sub></b>	<b>T+SWC : cE<sub>0</sub></b>
45	T : min_time <b>T : cE<sub>0</sub></b>	LI <b>T : cE<sub>0</sub></b>	LI, CI <b>T : cE<sub>0</sub></b>	LI, CI <b>T : cE<sub>0</sub></b>	T : annual <b>T+SWC : cE<sub>0</sub></b>	T : annual <b>T+SWC : cE<sub>0</sub></b>	<b>T+SWC : cE<sub>0</sub></b>	<b>T+SWC : cE<sub>0</sub></b>
55	T : min_time <b>T : cE<sub>0</sub></b>	<b>LI, CI</b> TxSWC : min_time	<b>LI, CI</b> T : cE <sub>0</sub>	<b>LI, CI</b> T : cE <sub>0</sub>	T : annual <b>T+SWC : cE<sub>0</sub></b>	T : annual <b>T+SWC : cE<sub>0</sub></b>	<b>T+SWC : cE<sub>0</sub></b>	<b>T+SWC : cE<sub>0</sub></b>
65	T : min_time <b>T : cE<sub>0</sub></b>	LI <b>T : cE<sub>0</sub></b>	LI, CI <b>T : cE<sub>0</sub></b>	LI, CI <b>T : cE<sub>0</sub></b>	T : annual <b>T+SWC : cE<sub>0</sub></b>	T : annual <b>T+SWC : cE<sub>0</sub></b>	<b>T+SWC : cE<sub>0</sub></b>	<b>T+SWC : cE<sub>0</sub></b>
75	T : cE <sub>0</sub>	LI <b>T : cE<sub>0</sub></b>	LI, CI <b>T : cE<sub>0</sub></b>	LI, CI <b>T : cE<sub>0</sub></b>	T : annual <b>T+SWC : cE<sub>0</sub></b>	T : annual <b>T+SWC : cE<sub>0</sub></b>	<b>T+SWC : cE<sub>0</sub></b>	<b>T+SWC : cE<sub>0</sub></b>
85	T : cE <sub>0</sub>	LI <b>T : cE<sub>0</sub></b>	LI, CI <b>T : cE<sub>0</sub></b>	LI, CI <b>T : cE<sub>0</sub></b>	T : annual <b>T+SWC : cE<sub>0</sub></b>	T : annual <b>T+SWC : cE<sub>0</sub></b>	<b>T+SWC : cE<sub>0</sub></b>	<b>T+SWC : cE<sub>0</sub></b>
95	T : cE <sub>0</sub>	LI <b>T : cE<sub>0</sub></b>	LI, CI <b>T : cE<sub>0</sub></b>	LI, CI <b>T : cE<sub>0</sub></b>	T : annual <b>T+SWC : cE<sub>0</sub></b>	T : annual <b>T+SWC : cE<sub>0</sub></b>	<b>T+SWC : cE<sub>0</sub></b>	<b>T+SWC : cE<sub>0</sub></b>
Survey (>99)	T : cE <sub>0</sub>	T : cE <sub>0</sub>	T : min_time <b>T : cE<sub>0</sub></b>	T : min_time <b>T : cE<sub>0</sub></b>	MA <b>T+SWC : cE<sub>0</sub></b>	MA <b>T+SWC : cE<sub>0</sub></b>	<b>T+SWC : cE<sub>0</sub></b>	<b>T+SWC : cE<sub>0</sub></b>

method yielded results in agreement with the RSME (Fig. 3).

The  $R^2$  for all gap filling techniques decreased with increasing gap fraction (Fig. 3). In the range of gap fractions from 5% to 95%, LI and T : cE<sub>0</sub> had the highest  $R^2$  (Table 2). At 99% gap fraction, the soil temperature method with a 308.56 K<sup>-1</sup> temperature sensitivity and varying  $R_{ref}$  had the highest  $R^2$ . At all gap fractions evaluated, the  $R^2$  for the T : annual, and T+SWC : cE<sub>0</sub> methods were the lowest, and at >99% gap fraction the MA method had the lowest  $R^2$ .

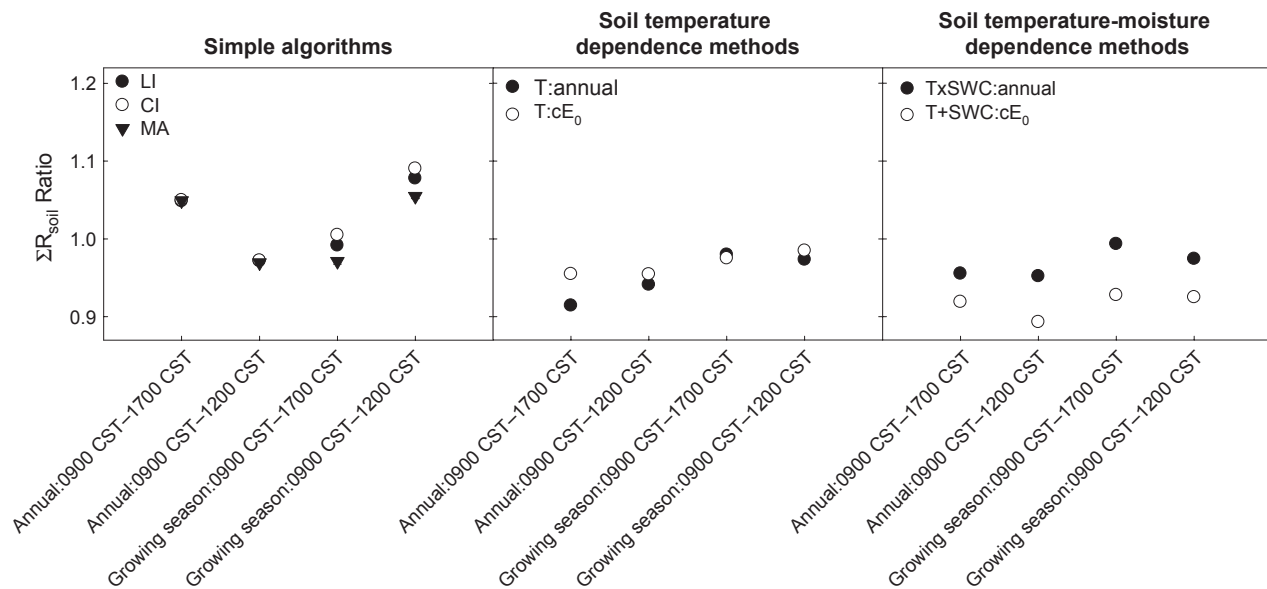
The BE refers to the error in  $\mu\text{mol CO}_2 \text{ m}^{-2} \text{ s}^{-1}$  introduced to the predicted half-hour  $R_{soil}$  data. Error increased with increasing the gap fraction for all the methods evaluated (Fig. 3), and was largest for the T : annual, T+SWC : cE<sub>0</sub> and TxSWC : annual methods (within a range of  $\pm 0.02$  to  $\pm 0.23 \mu\text{mol CO}_2 \text{ m}^{-2} \text{ s}^{-1}$  for 5% and >99% gap fractions, respectively; Fig. 3; Table 2). In contrast, the LI, CI, T : cE<sub>0</sub>, and TxSWC : min\_time methods had among the lowest BE at all gap fractions compared to the other methods ( $\pm 0.0002$  and  $\pm 0.11 \mu\text{mol CO}_2 \text{ m}^{-2} \text{ s}^{-1}$  for 5% and >99% gap fraction, respectively; Fig. 3; Table 2).

The ratio between the predicted and observed  $\Sigma R_{soil}$  represents the bias on the  $\Sigma R_{soil}$  introduced through gap filling. The statistical comparison between predicted and observed  $\Sigma R_{soil}$  allowed for the evaluation

of each method's performance (Table 2). For gaps of all lengths (5–95% gap fraction), the LI, CI, T : cE<sub>0</sub> and TxSWC : min\_time methods consistently had  $\Sigma R_{soil}$  ratio closest to 1 compared to the other gap filling techniques (Fig. 3). At >99% gap fractions, the soil temperature methods that filled gaps based upon a constant or subannual temperature-dependence (i.e. T : cE<sub>0</sub> and T : min\_time methods) had a ratio similar to 1. In contrast, the T : annual and T+SWC : cE<sub>0</sub> methods  $\Sigma R_{soil}$  ratio departed significantly from 1 at all gap fractions.

For the automated field measurements conducted for this study, the average  $\Sigma R_{soil}$  for the 20  $R_{soil}$  records was  $645 \text{ gC m}^{-2} \text{ y}^{-1}$ . The average gap fraction for these records was  $34 \pm 2\%$  (ranging from 16% to 48% missing data) depending upon year and ecosystem measured. Using the T : annual method with 100 permutations of artificial gap creation, the predicted uncertainty for the  $\Sigma R_{soil}$  was within a range of  $\pm 19 \text{ gC m}^{-2} \text{ y}^{-1}$  (Fig. 3). In contrast, for a gap fraction of 34% the soil temperature method with constant temperature sensitivity and varying  $R_{ref}$  estimated  $\Sigma R_{soil}$  within a range of  $\pm 1.9 \text{ gC m}^{-2} \text{ y}^{-1}$  (Fig. 3).

The soil temperature method assuming a  $E_0$  of  $308.56 \text{ K}^{-1}$  and varying  $R_{ref}$  yielded the most accurate estimates of  $\Sigma R_{soil}$  when  $R_{ref}$  was estimated from 0900 CST to 1700 CST and from 0900 CST to 1200 CST during



**Fig. 4** Average performance of three contrasting gap filling methods for various survey soil respiration schemes. Artificial gaps represent surveys occurring over two different time frames (0900 CST–1700 CST or 0900 CST–1200 CST) and two different portions of the year (entire year–Annual– or from April to October–Growing season). Values are means  $\pm$  standard error of the ratio of gap filled to real  $\Sigma R_{soil}$  ( $\Sigma R_{soil}$  ratio) for 20 records run 100 times each. Standard error values are smaller than symbols used for means. It is important to note that this metric represents the average performance of each method over multiple random gap permutations as opposed to the expected performance on any one gap scenario. Gap filling methods include the simple algorithms, soil temperature-dependence and soil temperature-moisture dependence methods and are abbreviated as in Table 1.



the growing season (Fig. 4). The  $\Sigma R_{\text{soil}}$  ratio for simple algorithm methods deviated least from 1 when  $R_{\text{soil}}$  was measured from 0900 CST to 1700 CST during the growing season (Fig. 4; 95% CI). For the growing season survey scheme from 0900 CST to 1700 CST, the LI and TxSWC : annual methods had a ratio similar to 1 (Fig. 4). At all survey schemes, the method with a ratio that significantly departed from 1 was the soil temperature-moisture method without interaction (Fig. 4).

## Discussion

In this study, we evaluated the performance of nine gap filling methods (Table 1) by analyzing the errors introduced when filling artificial gaps into  $R_{\text{soil}}$  datasets. The performance of these gap filling methods was assessed using various statistical metrics (RMSE,  $R^2$ , BE and  $\Sigma R_{\text{soil}}$  ratio). All methods performed best at lower gap fractions, and had relatively high, systematic errors for simulated survey measurements (Figs 2 and 3). For gap fractions between 5 and 95%, methods involving linear interpolation of  $R_{\text{ref}}$  or  $R_{\text{soil}}$  performed best (i.e. T : cE<sub>0</sub> and LI methods). For simulated survey measurements (>99% gap fraction), the T : cE<sub>0</sub> method performed best, although it tended to underestimate  $\Sigma R_{\text{soil}}$  by an average of 4% (Fig. 4). In contrast, methods that filled gaps based upon a single temperature-dependence or temperature- and moisture-dependence function (i.e. T : annual, TxSWC : annual, and T+SWC : cE<sub>0</sub> methods) performed relatively poorly at all gap fractions (Table 2). Indeed, the predicted uncertainty in  $\Sigma R_{\text{soil}}$  at 34% gap fraction using the T : annual method was twofold higher than the uncertainty in the  $\Sigma R_{\text{soil}}$  estimates calculated using the T : cE<sub>0</sub> method. These results indicate that the most commonly employed gap filling method (T : annual; Fig. 1) is not optimal, and that gap filling accuracy could be improved using easily applied methods for both automated and manual  $R_{\text{soil}}$  systems.

The differential performance of these gap filling methods can be understood based on the mechanisms driving soil respiration. Temperature is a primary driver of soil respiration and it is therefore no surprise that the method with best overall performance (T : cE<sub>0</sub>) is the one that accounted for temperature. The T : cE<sub>0</sub> method assumed a constant  $E_0$  while  $R_{\text{ref}}$  varied (see Eqn 1), as opposed to the other two temperature-dependent models that fit both  $E_0$  and  $R_{\text{ref}}$  at annual or subannual time frames (T : annual and T : min\_time). Although the temperature-dependence of  $R_{\text{soil}}$  often has been described using a constant temperature-sensitivity parameter (Lloyd & Taylor, 1994; Allen *et al.*, 2005; Reichstein *et al.*, 2005),  $E_0$  varies seasonally (Janssens & Pilegaard, 2003; Curiel-Yuste *et al.*, 2004; Suseela

*et al.*, 2012). Indeed, the theoretically expected temperature-dependence of aerobic respiration by microbes (e.g. Allen *et al.*, 2005) may be modified by many factors including substrate quality and supply, soil moisture, biophysical constraints, temperature-dependence of resource supply, and secretion of extracellular enzymes with a lower temperature-sensitivity (Davidson & Janssens, 2006; Allison *et al.*, 2010; O'Brien *et al.*, 2010; Wallenstein *et al.*, 2011; Anderson-Teixeira & Vitousek, 2012; Gomez-Casanovas *et al.*, 2012).

In addition, the temperature sensitivity of root respiration can be influenced by changes in plant carbon allocation patterns between the above- and the belowground component, root biomass, soil moisture and thermal acclimation of respiration (Kucera & Kirkham, 1971; Carbone & Trumbore, 2007; Drake *et al.*, 2008; Wang *et al.*, 2010). Our results showed that for the purposes of gap filling, it was almost always preferable to assume a constant  $E_0$  (i.e. T : cE<sub>0</sub>) than to attempt statistical estimation of  $E_0$  over the minimum possible time frame (i.e. T : min\_time method; detailed in Appendix S2; Figs 2–3, Table 2). This does not necessarily imply that  $E_0$  is constant but that a reasonable approximation of the physiological temperature-dependence of  $R_{\text{soil}}$  coupled with linear interpolation of  $R_{\text{ref}}$  provides the best statistical fit. Further research will be required to understand the degree to which  $E_0$  actually matches the assumed value ( $E_0 = 308.56 \text{ K}^{-1}$  in Eqn 1  $\approx E_a = 0.62 \text{ eV}$  in Arrhenius equation  $\approx Q_{10} = 2.4$ ) over short-time frames (i.e. days to weeks), as is required to disentangle the temperature sensitivity of  $R_{\text{soil}}$  from confounding factors.

When both  $E_0$  and  $R_{\text{ref}}$  were fit statistically (T : min\_time method), gap filling performance should be optimized by minimizing the time frame over which the  $R_{\text{soil}}$ -temperature relationship (Eqn 1) was fit (T : min\_time method; Figs 2–3; Table 2). This result makes sense in light of the fact that both  $E_0$  and  $R_{\text{ref}}$  can vary seasonally in response to changes in plant phenology, root or microbial biomass, microbial composition, and soil moisture (Janssens & Pilegaard, 2003; Suseela *et al.*, 2012). Therefore, estimates of  $E_0$  and  $R_{\text{ref}}$  calculated over long periods of time (i.e. the entire year as in the T : annual method) can reflect confounding factors such as phenology effects on soil respiration that may alter these parameters (Reichstein *et al.*, 2005). Gap filling methods that estimate  $E_0$  and  $R_{\text{ref}}$  over short periods of time should theoretically reduce confounding effects in  $E_0$  and  $R_{\text{ref}}$  estimates. Particularly at lower gap fractions ( $\leq 65\%$ ) where there were sufficient data to fit Eqn 1 over short time frames, the T : min\_time method was among the most accurate gap filling approaches (Fig. 3, Table 2), indicating its success at representing seasonal variation in  $E_0$  and  $R_{\text{ref}}$ . For simulated survey records (>99% gap fraction), however, there were insuf-

ficient data for this method to create a unique fit; rather, it fit a single relationship for the entire year and defaulted to an LI fit if the fit was unreasonable (this gave this method the advantage over T : annual at the highest gap fraction; Fig. 3, Table 2).

In contrast to the T : min\_time method, the T : annual method assumed that the  $R_{\text{soil}}$ -temperature relationship (Eqn 1) could be represented by a fit over the entire year. Because fitting a temperature-dependence relationship over an entire year can result in a strongly biased estimate of  $E_0$  (Reichstein *et al.*, 2005), it is not surprising that this method was among the poorest performers (Fig. 3, Table 2). Particularly at the highest gap fractions, the T : annual method tended to underestimate  $R_{\text{soil}}$ . Underestimates in  $R_{\text{soil}}$  were likely caused by generally high  $E_0$  ( $E_0 = 300\text{--}470 \text{ K}^{-1}$ ) with consequent low  $R_{\text{ref}}$  estimates as calculated  $R_{\text{soil}}$  depends on both  $E_0$  and  $R_{\text{ref}}$ . The relatively poor performance of this method is notable, given that it has been the most widely used for gap filling in the past (Fig. 1). Our analysis indicates that annual  $R_{\text{soil}}$  estimates could be significantly improved by using the T :  $cE_0$  method in place of the T : annual method (Fig. 3, Table 2).

Soil moisture plays an important role in the regulation of  $R_{\text{soil}}$  (e.g. Reichstein *et al.*, 2003); however, methods incorporating  $RSWC$  (TxSWC : annual, T+SWC :  $cE_0$ , and TxSWC : min\_time) generally did not perform well (Table 2). There are two potential explanations for this relatively weak performance. First, because our study site is relatively mesic, soil moisture was not strongly limiting  $R_{\text{soil}}$  most of the time. In fact, the relationship between  $R_{\text{ref}}$  and  $RSWC$  at an annual time scale (T+SWC :  $cE_0$  method) often was slightly negative or zero (data not shown), indicating that  $R_{\text{soil}}$  was more often unaffected or slightly reduced by excessive soil moisture than limited by dry conditions. Second, incorporating another predictive variable into gap filling methods may increase the predictive power when gap fractions are relatively low – as indicated by the superior performance of TxSWC : annual over T : annual and TxSWC : min\_time over T : min\_time at low gap fractions (Table 2), but this also increases the prevalence of unreasonable fits – particularly when data are limiting. Indeed, at gap fractions of 25% and higher, TxSWC : annual was consistently among the poorest performers in terms of accuracy (RMSE and  $R^2$ ; Table 2). Particularly at higher gap fractions, the TxSWC : min\_time method failed to produce reasonable predictions and defaulted to the LI fit. It is for this reason that TxSWC : min\_time closely parallels LI, particularly at higher gap fractions (Fig. 3, Table 2), and, therefore, the success of TxSWC : min\_time is generally not derived from the success of this model *per se*.

The strong performance of the gap filling techniques that use interpolation to estimate  $R_{\text{soil}}$  or  $R_{\text{ref}}$  (LI, CI, and T :  $cE_0$ ) indicates that factors in addition to temperature and soil moisture were important predictors of  $R_{\text{soil}}$ . By assuming that missing values were best predicted by their nearest neighbors these methods effectively integrate several factors that may influence  $R_{\text{soil}}$  (Brüggemann *et al.*, 2011), including above and below ground partitioning (e.g. Carbone & Trumbore, 2007), labile C inputs from plant roots (Badri & Vivanco, 2009), the quantity, and quality of soil organic carbon (Kirschbaum, 1995), soil nitrogen availability (e.g. Janssens *et al.*, 2010), and measurement bias (e.g. minor, undetected equipment problems). The fact that  $R_{\text{ref}}$  was better predicted by nearest-neighbor measurements than by models that included soil moisture (i.e. comparing methods T :  $cE_0$  and T+SWC :  $cE_0$ ; Table 2) indicates that the contribution of soil moisture to  $R_{\text{ref}}$  was relatively small at our site. The relative performance of techniques predicting  $R_{\text{ref}}$  based on linear interpolation and  $RSWC$  (i.e. T :  $cE_0$  and T+SWC :  $cE_0$ , respectively) may differ at semiarid or tropical sites where soil moisture more strongly affects  $R_{\text{soil}}$ .

Because of the extremely low measurement frequency, the most challenging gap filling scenario is estimating annual  $R_{\text{soil}}$  from a survey measurement record. All gap filling methods had low accuracy and high bias error when applied to >99% gap fractions (Fig. 3). The simple algorithm methods which make no correction based on temperature overestimated  $R_{\text{soil}}$  by on average ca. 5% (Fig. 3). In contrast, methods that incorporate a temperature-dependence systematically underestimated  $R_{\text{soil}}$  by on average ca. 5–12% (with the exception of TxSWC : min\_time, as it defaulted to LI) (Fig. 3). Underestimates in  $\Sigma R_{\text{soil}}$  with soil temperature-dependence methods are likely driven by overestimates of  $E_0$  and consequent underestimation of  $R_{\text{ref}}$ . This implies that factors other than temperature and moisture may be limiting  $R_{\text{soil}}$  and thus influencing the temperature sensitivity of  $R_{\text{soil}}$  (Davidson *et al.*, 2006; Gomez-Casanovas *et al.*, 2012).

The performance of gap filling methods for estimating annual  $R_{\text{soil}}$  based upon a survey measurement record interacted with the timing of measurements (e.g. 0900 CST–1700 CST or 0900 CST–1200 CST; Fig. 4) and whether measurements are made during the entire year or only during the growing season (April–October for our research sites; Fig. 4). The simple algorithm methods were strongly dependent upon the extent to which survey measurements were representative of average daily  $R_{\text{soil}}$  (Fig. 4). Therefore, if daily measurements are timed to represent average daily  $R_{\text{soil}}$ , annual estimates will be quite accurate. The methods that incorporated temperature and moisture-dependence were sensitive to the timing of measurements (Fig. 4). On average,

these methods underestimated  $R_{\text{soil}}$  at all survey time frames. However, the soil temperature method with constant  $E_0$  but varying  $R_{\text{ref}}$  performed best at survey schemes where  $R_{\text{ref}}$  was estimated during the growing season from 0900 CST to 1200 CST and from 0900 CST to 1700 CST (Fig. 4). These results imply that  $R_{\text{ref}}$  calculated over these time frames are representative of the daily  $R_{\text{ref}}$  estimates yielding good predictions of the daily  $R_{\text{soil}}$  flux.

Additional research is needed to understand the variables that influence  $R_{\text{ref}}$ , as this is fundamental to understanding the mechanisms that determine the temperature sensitivity of  $R_{\text{soil}}$ . This analysis of various gap filling strategies sets the basis for selecting optimal gap filling methods for accurate estimates of  $\Sigma R_{\text{soil}}$ . In general, the most accurate gap filling method for automated records among those evaluated here was T : cE<sub>0</sub>, which assumed a constant  $E_0$  and filled gaps in  $R_{\text{ref}}$  using linear interpolation (Fig. 3, Table 2; details in Appendix S2). Another advantage of this method is that it is computationally simple. If a complete soil temperature record is not available, linear interpolation (LI) was the most accurate method among the simple algorithms and was almost as accurate as T : cE<sub>0</sub>. In ecosystems where soil moisture is a critical driver of  $R_{\text{soil}}$ , methods accounting for soil moisture may be most appropriate, particularly if soil moisture varies dramatically on time scales shorter than the average gap length. From this analysis, it appears that the TxSWC : annual method may provide a better fit than T+SWC : cE<sub>0</sub> (Fig. 3, Table 2), and this method would be theoretically expected to perform better in strongly water-limited systems as it captures the previously observed increase in  $E_0$  with RSWC (Eqn 2; Reichstein *et al.*, 2003). The TxSWC : min\_time method did not provide accurate estimates of  $\Sigma R_{\text{soil}}$ , but it may perform better in highly water-limited systems. Determination of the best gap filling method for semiarid and tropical systems will require an analysis of the type presented here.

The time of day and time of year of survey measurements were important for accurate extrapolation to  $\Sigma R_{\text{soil}}$  (Fig. 4), and the daily representative  $R_{\text{soil}}$  fluxes will likely depend upon site and vary over time. Therefore, we recommend carefully scheduling surveys to represent the average daily  $R_{\text{soil}}$  for the T : cE<sub>0</sub> and LI method (Fig. 4).

This analysis provides guidance as to optimal techniques for estimating reliable  $\Sigma R_{\text{soil}}$  and sheds light on the mechanisms driving soil respiration. On the basis of this analysis, we recommend a shift away from the most widely used gap filling method (T : annual; Fig. 1), which was among the most poorly-performing methods evaluated here. We show

that alternative methods, particularly T : cE<sub>0</sub> and LI are significantly more reliable. Improved and standardized techniques for estimation of annual  $R_{\text{soil}}$  will be valuable for comparing across sites and understanding the role of soil respiration in ecosystem- to global-scale C cycles.

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### Supporting Information

Additional Supporting Information may be found in the online version of this article:

**Appendix S1.** Reference list used for the literature search on published strategies used to gap fill  $R_{soil}$  records.

**Appendix S2.** Description of gap filling methods.