



Graph-based Rare Category Analysis: Exploration, Exploitation, and Interpretation

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Rare Categories in the Real World...



1. Insider Threat



Self-Similarity



3. Lone Wolf Terrorism



4. Gene Disease



5. Identity Theft



6. Emerging Trend

- Workshop on Challenges and Opportunities for AI in Financial Services: the Impact of Fairness, Explainability, Accuracy, and Privacy, Co-located with NIPS 2018.
- Workshop on Anomaly Detection in Finance, Co-located with KDD 2017.
- Spaaij, R.. "The enigma of lone wolf terrorism: An assessment." *Studies in Conflict & Terrorism* 33.9 (2010): 854-870.
- Ngai, E. W., Hu, Y., Wong, Y. H., Chen, Y., & Sun, X. The application of data mining techniques in financial fraud detection: A classification framework and an academic review of literature. *Decision support systems*, 50(3), 559-569.

Malicious Insiders

Malicious Insider



Definition

Current or former employee or contractor who

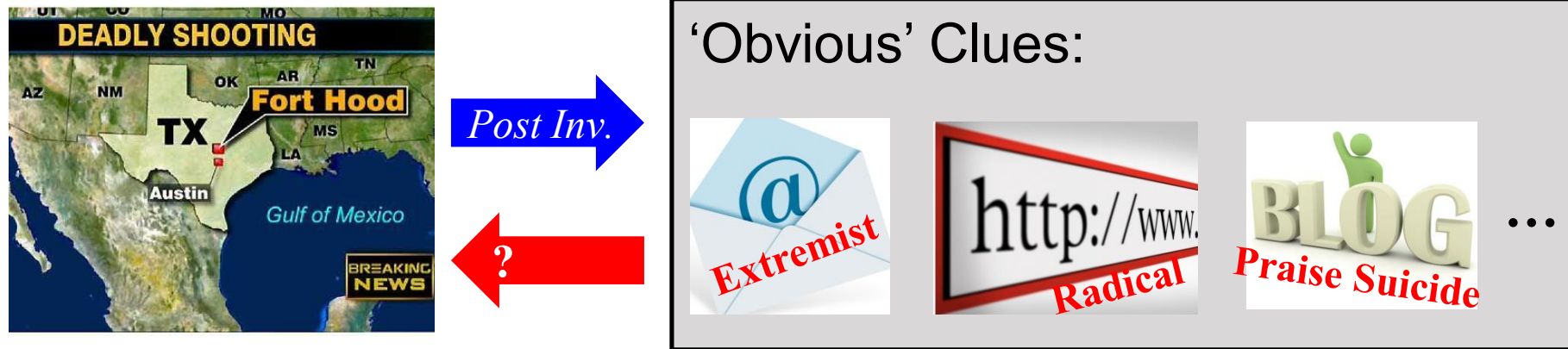
- **intentionally** exceeded or misused an authorized level of network, system or data access in such a way that,
- **affected** the security of the organizations' data, systems, or daily business operations

[Cappelli et al, RSA2008]

Hard to identify → Insiders often camouflage themselves...

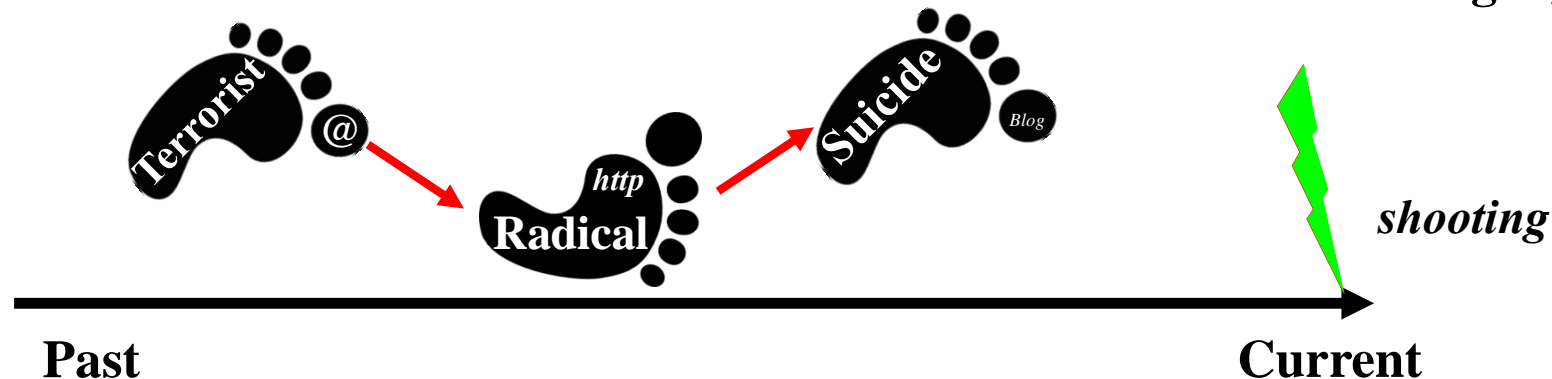
DARPA-BAA-10-84, DARPA-BAA-11-04, DARPA-BAA-11-64, IARPA-BAA-12-01, ...

Malicious Insiders: Fort Hood Shooting



Q: Can we reverse it?

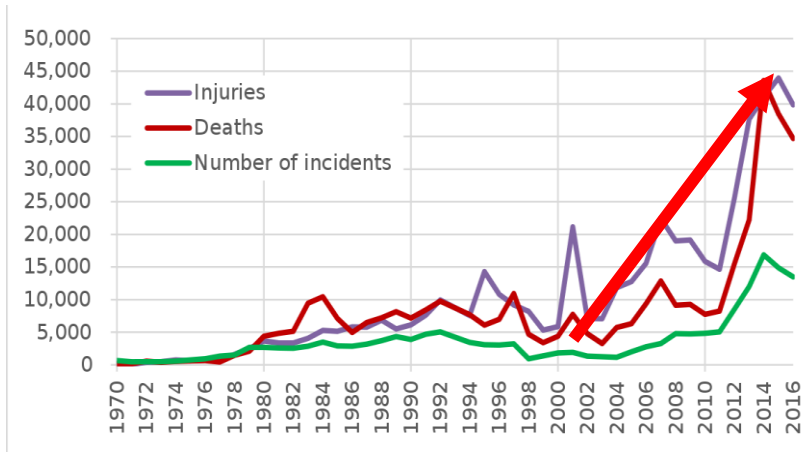
G1. Find individual traces *G2*. Connect the dots *G3*. Prevent the tragedy



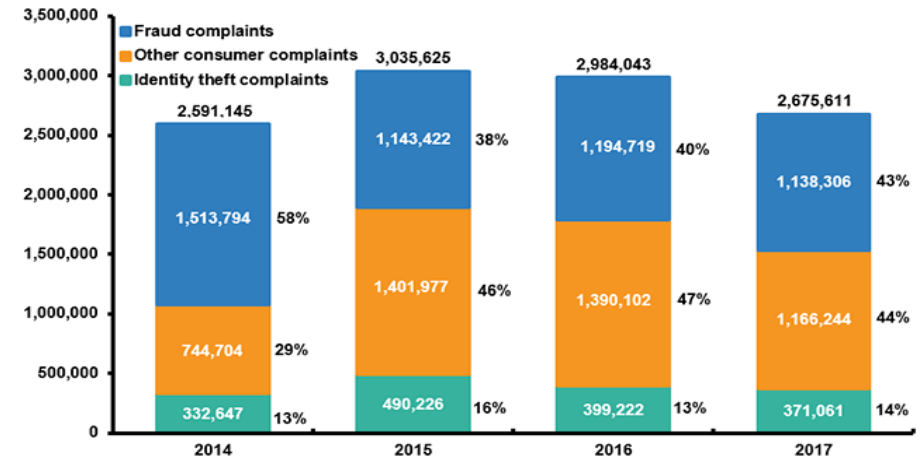
How to find more insiders of the same type?

Why Do We Care?

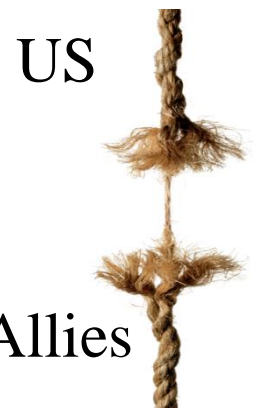
Terrorist Events Worldwide



Financial Fraud [Federal Trade Commission, 2017]



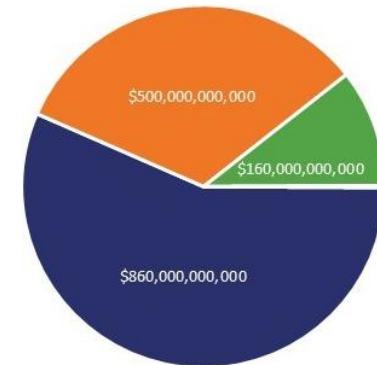
PR Crisis



US

Allies

Cybercrime [M., McGuire, RSA2018]

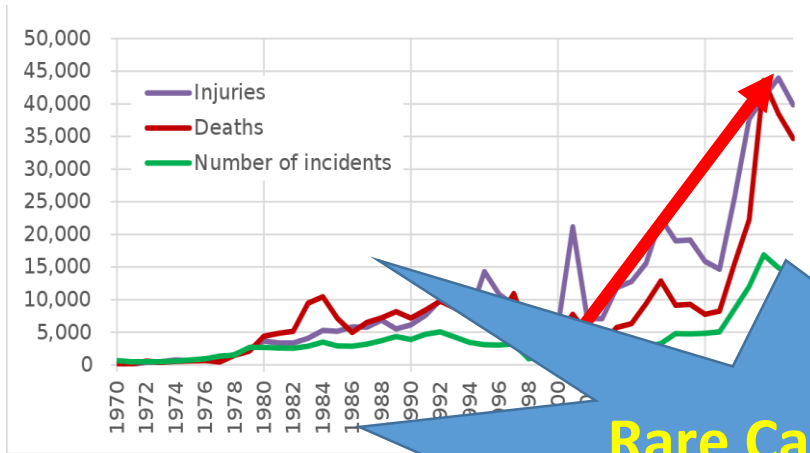


- Illegal online markets
- Trade secret, IP theft
- Data Trading

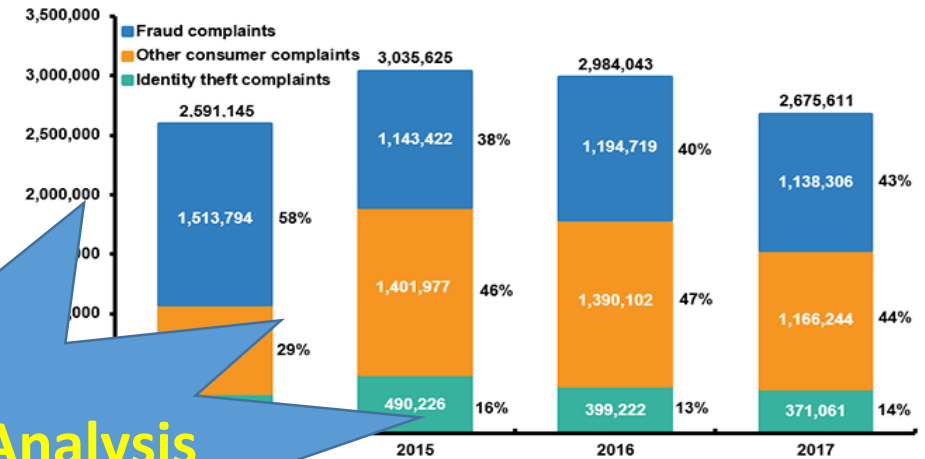
Cost over 1.5 trillion in 2018

Why Do We Care?

Terrorist Incidents Worldwide

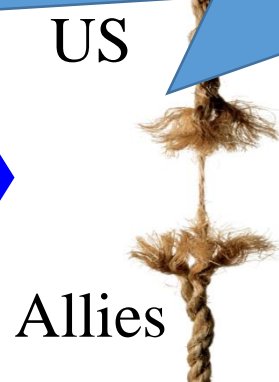


Financial Fraud [Federal Trade Commission, 2017]

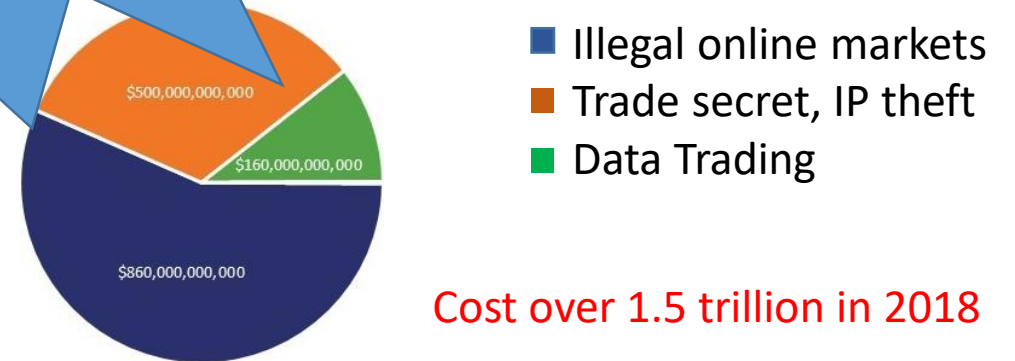


Rare Category Analysis (RCA)

PR Crisis



McGuire, RSA2018]



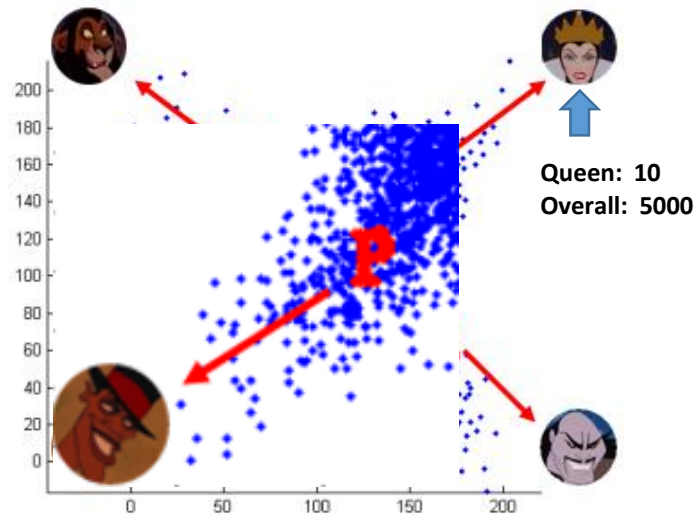
Cost over 1.5 trillion in 2018

Rare Category Analysis

- Problem Definition

Rare category analysis (RCA) refers to the problem of **detecting**, **characterizing**, **representing** and **interpreting** rare examples from *underrepresented* minority classes in an *imbalanced* data set.

- An Illustrative Example



- **Imbalanced** data set
- Minority classes are **not separable** from majority class

Comparison with Imbalanced Classification

- Imbalanced Classification

- Problem definition

- Labeled examples from all the classes

- Models for imbalanced classification focus on **overall accuracy** of all classes

- **Methodology:** [Kubat & Matwin, ICML1997]; [Chawla et al, JAIR2002]; [Wu & Chang, ICML2003]; [Huang et al., CVPR2016]; ...

- Rare Category Analysis

- Problem definition

- None/one/few-shot labeled example from the rare categories

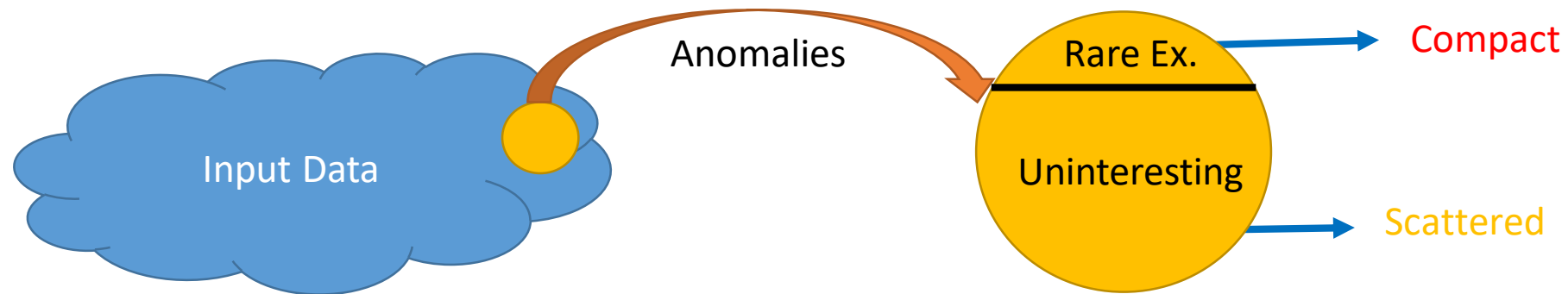
- Models for rare category analysis put heavy emphasis on **learning minority classes** with a good performance.

- **Methodology:** [Fine & Mansour, COLT2006]; [Dasgupta & Hsu, ICML2008]; [Vatturi & Wong, KDD2009]; [Zhou et al., KDD2018]; ...

Comparison with Outlier/Anomaly Detection

- **Outliers/Anomalies**
 - Patterns in data that do not conform to expected behavior [Chandola, Banerjee & Kumar, 2009]
 - Typically separable from normal examples and **scattered** in the feature space
- **Rare Categories**
 - **Compact** in the feature space, may **overlap** with the majority class [He, 2010]
- **Outliers/Anomalies vs. Rare Categories**

“Most of the objects (i.e., **majority classes**) are well explained by current theories and ... remainder are anomalies, but 99% of these anomalies are **uninteresting (i.e., boring anomalies)**, and only **1% of them (i.e., rare categories)** are **useful**” [Pelleg & Moore, 2004]



- V. Chandola, A. Banerjee, V. Kumar: Anomaly Detection: A Survey. ACM Comput. Surv. 41(3): 15:1-15:58 (2009).
- J. He (2010). Rare category analysis (Doctoral dissertation, Carnegie Mellon University, School of Computer Science, Machine Learning Department).
- D. Pelleg, A. W. Moore: Active Learning for Anomaly and Rare-Category Detection. NIPS 2004.

Example: Sloan Digital Sky

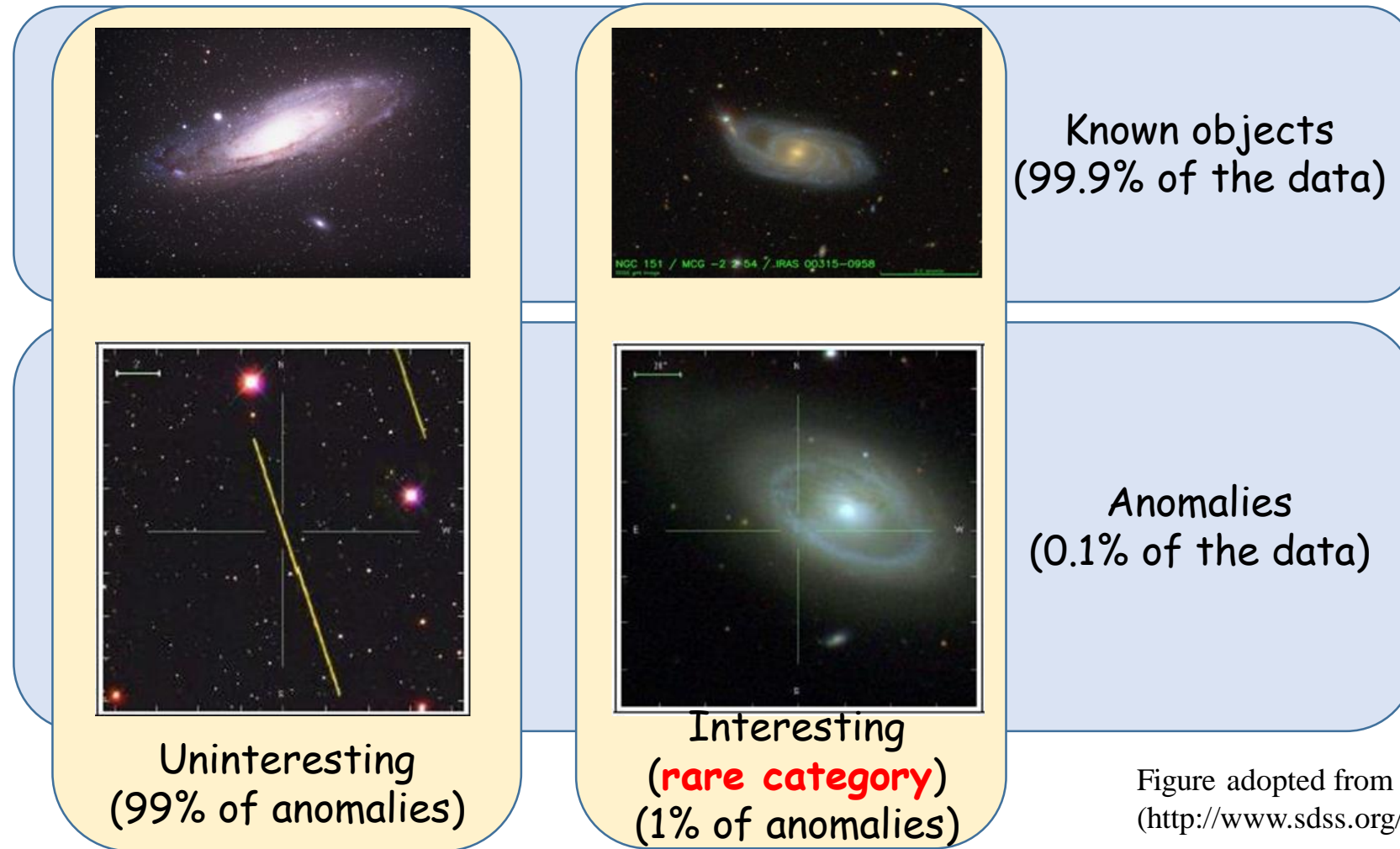


Figure adopted from Sloan Digital Sky Survey
(<http://www.sdss.org/iotw/archive.html>)

Key Challenge #1: Rarity

Highly-skewed distribution

- *0.1%* of any given population of users is malicious
- *99.9%* are normal users

[DARPA-BAA-11-04]

Commonality of insiders

- Detecting insiders of each type
- Identifying relevant features
- Characterizing each type of insiders

Non-separable nature

- Malicious users often camouflage their abnormal behaviors
- Malicious users try to bypass the detection systems

QI: How to detect and characterize insiders of each type, using as little cost as possible?

Key Challenge #2: Dynamics

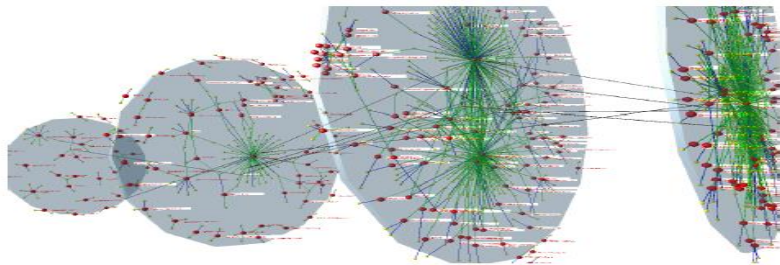
Low-footprint of insiders

- *0.1%* of any given population of users is malicious
 - *20%* of malicious insiders are active on any given day
- [DARPA-BAA-11-04]

Costly access to oracle

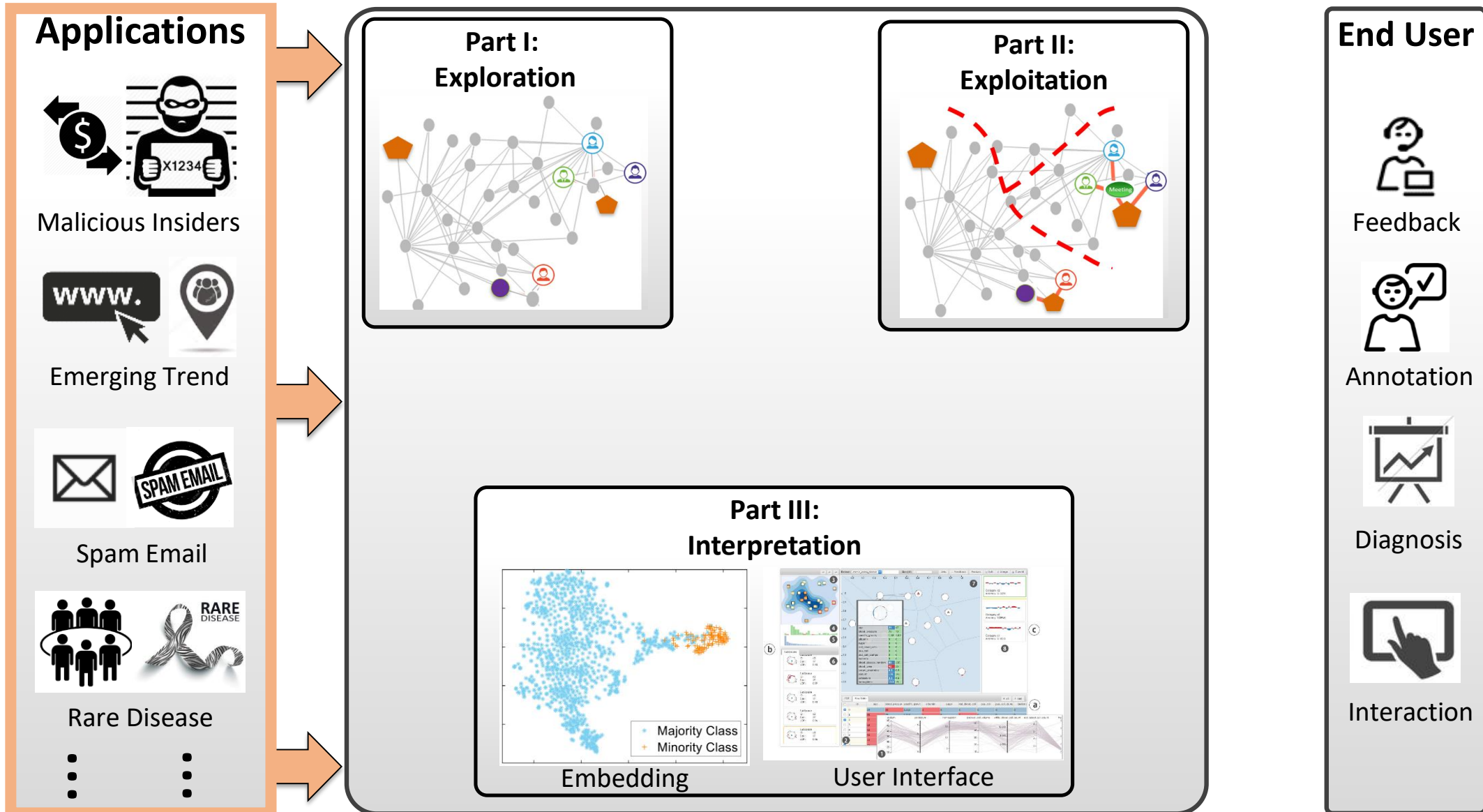
- [Fort Hood Shooting]
 - ✓ *65K* personnel at Fort Hood
 - 4.7B emails in 2 years
 - ✓ *~60* initial activity reviews per day per operator

Fine-grained dynamics



Q2: How to predict and track insiders of each type over time at the proper granularity?

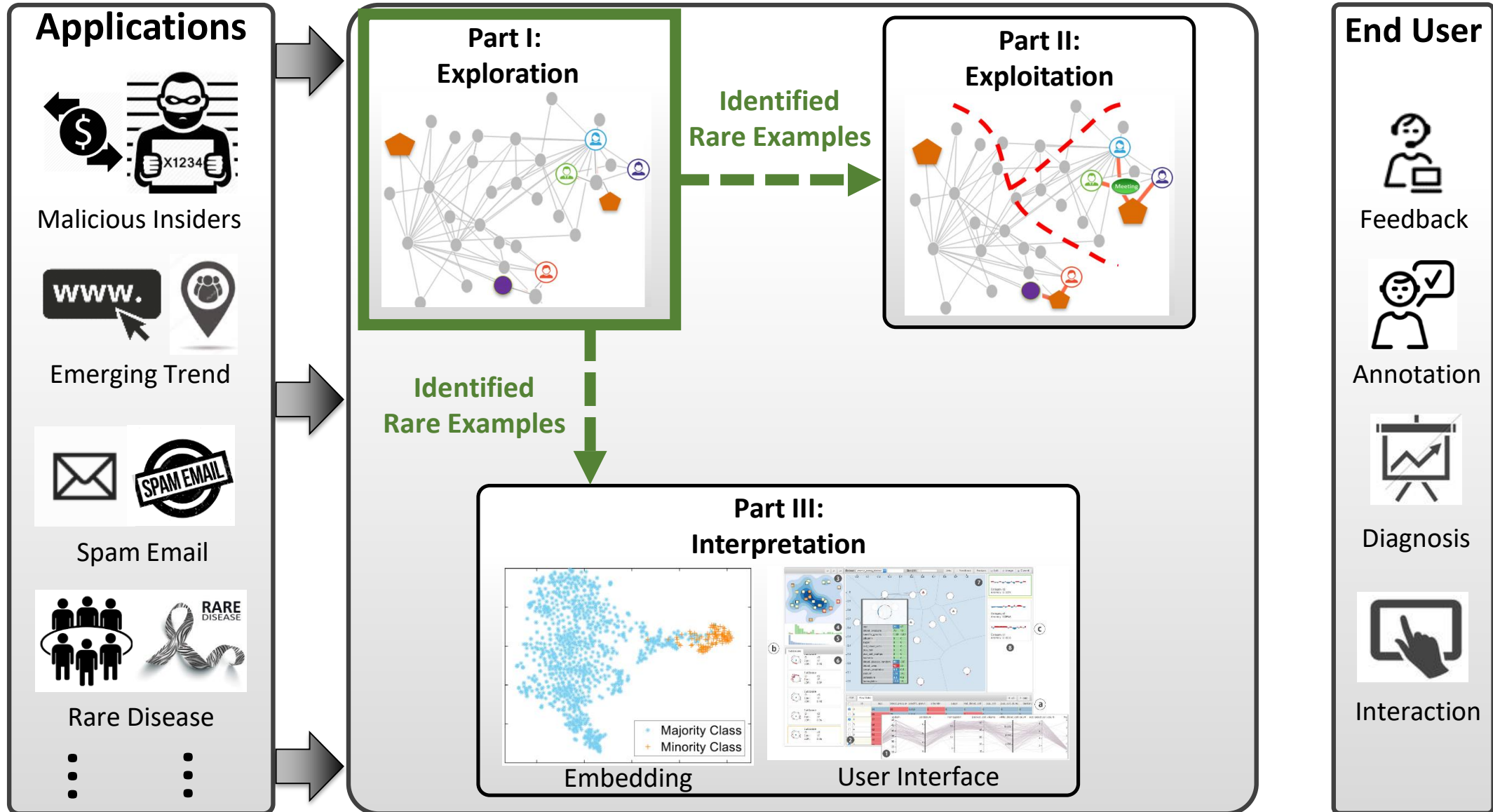
Overview of Complex Rare Category Analysis





**Part I:
Rare Category Exploration**

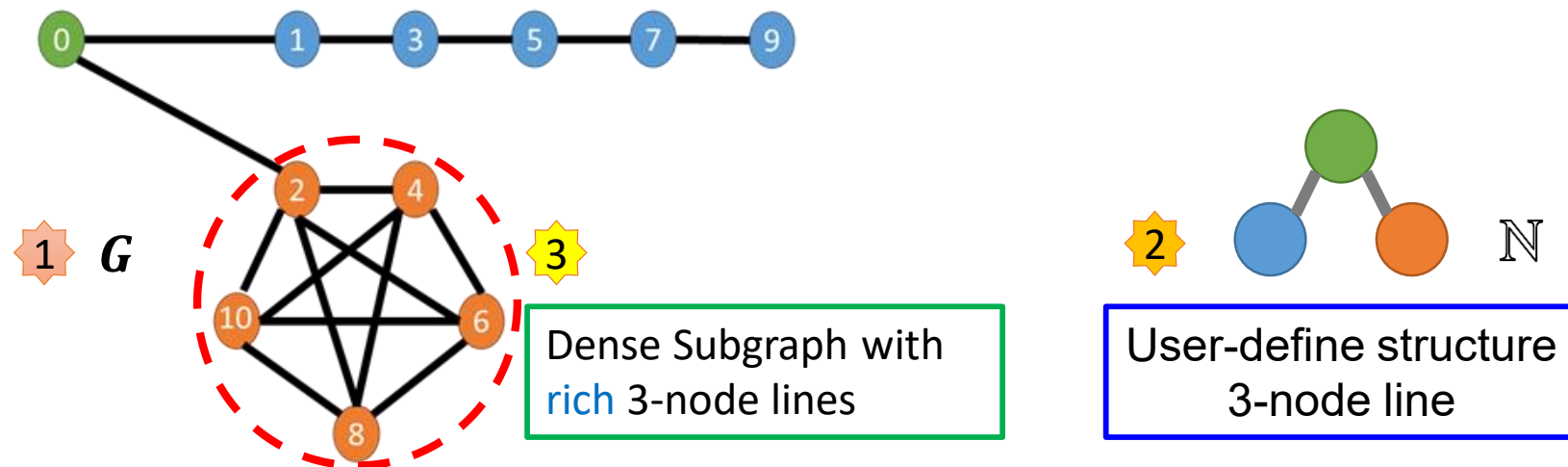
Overview of Complex Rare Category Analysis



Rare Category with High-Order Structures

• Specific Problem Definition

- Given: Graph $G=(V, E)$, user-defined structure \mathbb{N} .
- Find: A structure-rich dense subgraph that largely preserves the user-defined structures.



High-Order Structures in Real Applications



Stars



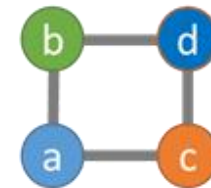
Internet



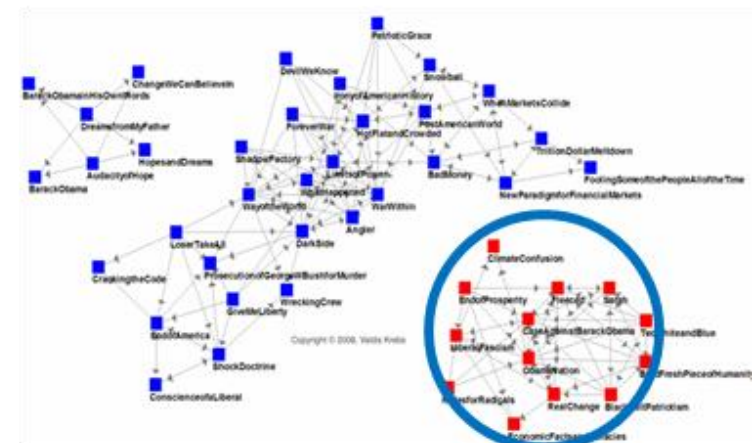
Triangles



Social Network



Loops



Online Transaction

High Order Conductance

• Definition

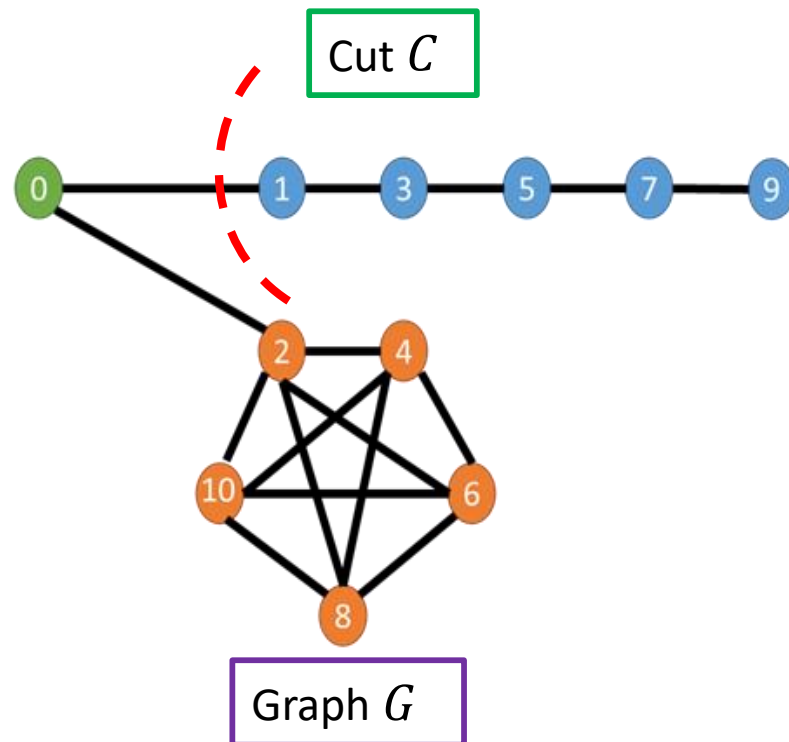
For any cluster C in graph G and the k^{th} -order structure \mathbb{N} , the k^{th} -order conductance $\Phi(C, \mathbb{N})$ is defined as

$$\Phi(C, \mathbb{N}) = \frac{\text{cut}(C, \mathbb{N})}{\min\{\mu(C, \mathbb{N}), \mu(\bar{C}, \mathbb{N})\}}$$

The diagram illustrates the components of the conductance formula. Red boxes and arrows provide definitions for the terms used:

- cut(C, N)**: The number of network structures \mathbb{N} broken due to the partition of G into C and \bar{C} .
- $\mu(C, \mathbb{N})$: The number of network structures \mathbb{N} in C .
- $\mu(\bar{C}, \mathbb{N})$: The number of network structures \mathbb{N} in \bar{C} .

Conductance vs. High Order Conductance



$$\Phi(C, \mathbb{N}) = \frac{\text{cut}(C, \mathbb{N})}{\min\{\mu(C, \mathbb{N}), \mu(\bar{C}, \mathbb{N})\}}$$

➤ Conductance



$$\Phi(C, \mathbb{N}) = \frac{1}{\min\{4, 11\}} = 1/4$$

➤ High-order conductance



$$\Phi(C, \mathbb{N}) = \frac{2}{\min\{3, 34\}} = \frac{2}{3}$$

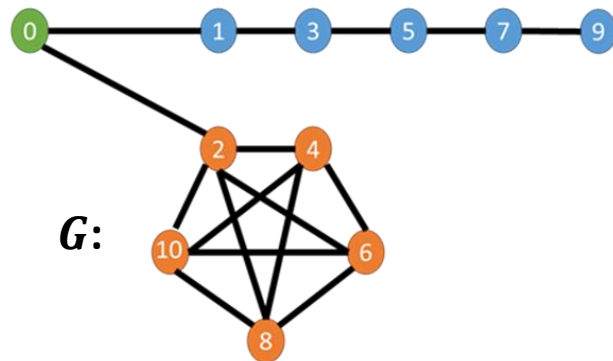
HOSPLOC Algorithm

- **Construct Adjacency Tensor**

Given a graph $G = (V, E)$, the k^{th} -order network structure \mathbb{N} on G could be represented in a k -dimensional adjacency tensor T as follows

$$T(i_1, i_2, \dots, i_k) = \begin{cases} 1 & \{i_1, i_2, \dots, i_k\} \subseteq V \text{ and form } \mathbb{N}. \\ 0 & \text{Otherwise.} \end{cases}$$

Example:



For the set of nodes {2, 4, 1}

$$T(1,4,2) = 0$$



For the set of nodes {6, 8, 10}

$$T(10,8,6) = 1$$



HOSPLOC Algorithm

- Compute Transition Tensor

Given a graph $G = (V, E)$ and the adjacency tensor T for the k^{th} -order network structure \mathbb{N} , the corresponding transition tensor P could be computed as

$$P(i_1, i_2, \dots, i_k) = \frac{T(i_1, i_2, \dots, i_k)}{\sum_{i_1=1}^n T(i_1, i_2, \dots, i_k)}$$

Example:

- Compute Transition Tensor

Given a graph $G = (V, E)$ and the adjacency tensor T for the k^{th} -order network structure \mathbb{N} , the corresponding transition tensor P could be computed as

G :

\mathbb{N} :



For the set of nodes $\{2, 4, 1\}$

$$P(1, 4, 2) = 0$$



For the set of nodes $\{6, 8, 10\}$

$$P(10, 8, 6) = 1/3$$

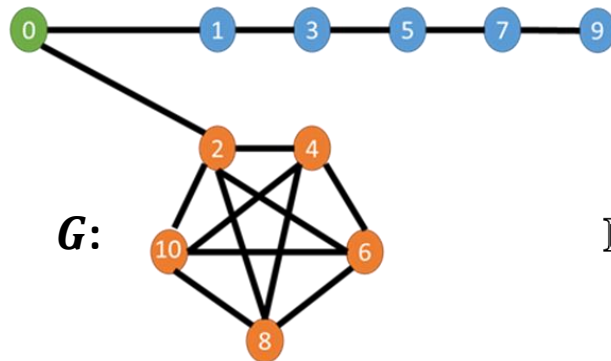


HOSPLOC Algorithm

- k^{th} -order Markov Chain Interpretation
 - Each vertex represents an individual state
 - Depends on the last $k-1$ states (nodes)

$$P(i_1, \dots, i_k) = \Pr(S_{t+1} = i_1 | S_t = i_2, \dots, S_{t-k+2} = i_k)$$

Example:



For the set of nodes $\{2, 4, 1\}$

$$P(1,4,2) = \Pr(v_1 | v_4, v_2) = 0$$



For the set of nodes $\{6, 8, 10\}$

$$P(10,8,6) = \Pr(v_{10} | v_6, v_8) = 1/3$$



HOSPLOC Algorithm

- High-Order Random Walk

- Using the "rank-1" approximation [Li and NG, 2013], the high-order random walks can be formulated as

$$q^{(t)} = P q^{(t-1)} \dots q^{(t-k+1)}$$

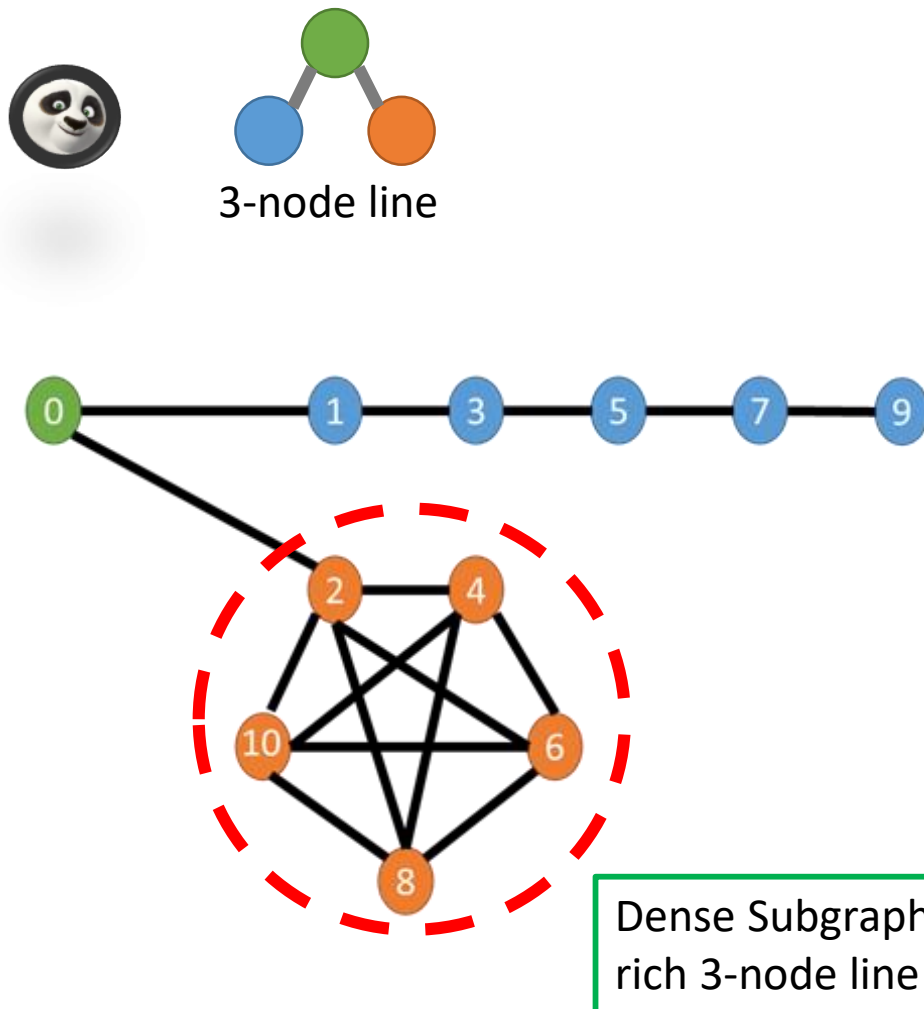
- Vector Based Graph Cut

- Locally conduct high-order random walks to explore \mathbb{N} .
- Compute the permutation π of the returned HRW distribution q such that:

$$\frac{q(\pi(1))}{d(\pi(1))} \leq \frac{q(\pi(2))}{d(\pi(2))} \leq \dots \leq \frac{q(\pi(n))}{d(\pi(n))}.$$

- Iteratively check the potential cuts C_1, C_2, \dots, C_{n-1} , where $C_i = \{\pi(1), \dots, \pi(i)\}$.

HOSPLOC Algorithm



Algorithm 1 High-Order Structure-Preserved Local Clustering (HOSPLOC)

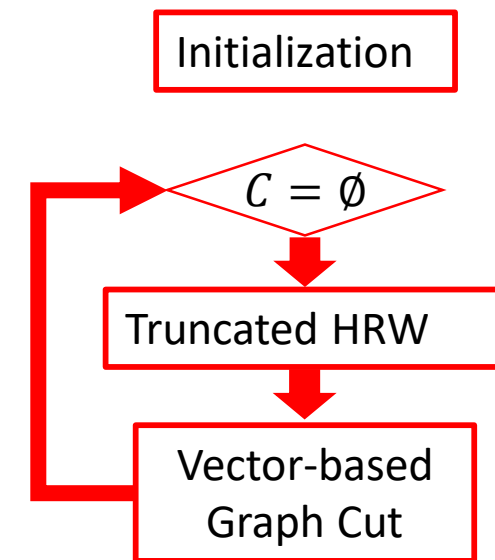
Input:

- (1) Transition tensor \mathbf{P} and transition matrix M ,
- (2) Initial vertex v ,
- (3) Conductance upper bound ϕ ,
- (4) Maximum iteration number t_{\max} ,
- (5) Parameters b, c_1, ξ .

Output:

Local cluster C :

- 1: Construct the unfolding matrix \tilde{P} of the transition tensor \mathbf{P} .
- 2: Compute constant ϵ based on Eq. 3.
- 3: Set initial distribution vectors $q^{(t)} = M^{(t-1)}\chi_v$, where $t = 1, \dots, k-1$.
- 4: Compute truncated initial local distribution vectors $r^{(t)} = [q^{(t)}]_{\epsilon}$, $t = 1, \dots, k-1$.
- 5: **for** $t = k : t_{\max}$ **do**
- 6: Update distribution vector $q^{(t)} = P(r^{(t-1)} \otimes \dots \otimes r^{(t-k+1)})$.
- 7: Update truncated distribution vectors $r^{(t)} = [q^{(t)}]_{\epsilon}$.
- 8: **if** there exists a j such that: **then**
- 9: (a) $\Phi(S_j(q^{(t)})) \leq \phi$,
- 10: (b) $2^b \leq \lambda_j(q^{(t)})$,
- 11: (c) $J_X(q^{(t)}, 2^b) \geq \frac{\xi}{c_1(t+2)2^b}$.
- 12: return $C = S_j(q^{(t)})$ and quit.
- 13: **else**
- 14: Return $C = \emptyset$.
- 15: **end if**
- 16: **end for**



Experimental Results

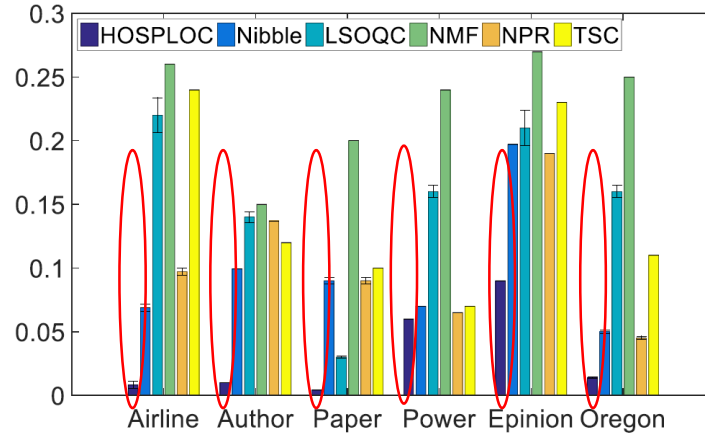
- Datasets

Category	Network	Type	Nodes	Edges
Citation	Author	Undirected	61,843	402,074
	Paper	Undirected	62,602	10,904
Infrastructure	Airline	Undirected	2,833	15,204
	Oregon	Undirected	7,352	15,665
	Power	Undirected	4,941	13,188
Social	Epinion	Undirected	75,879	508,837
Review	Rating	Bipartite	8,724	90,962
Financial	PII	Multipartite	375	519

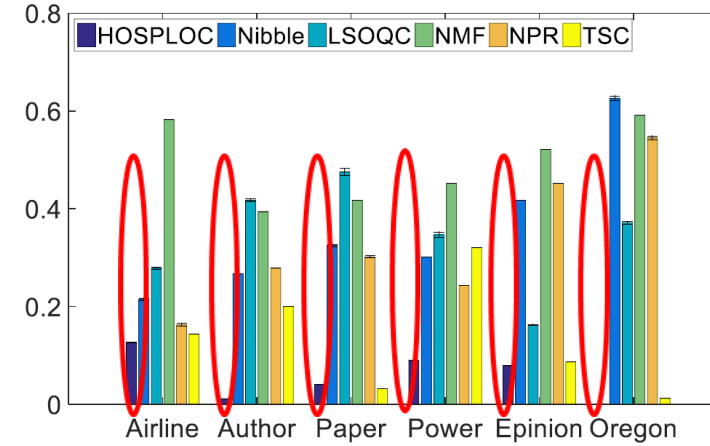
Effectiveness Analysis

Worse
↓
Better

(a) $\Phi(C, edge)$

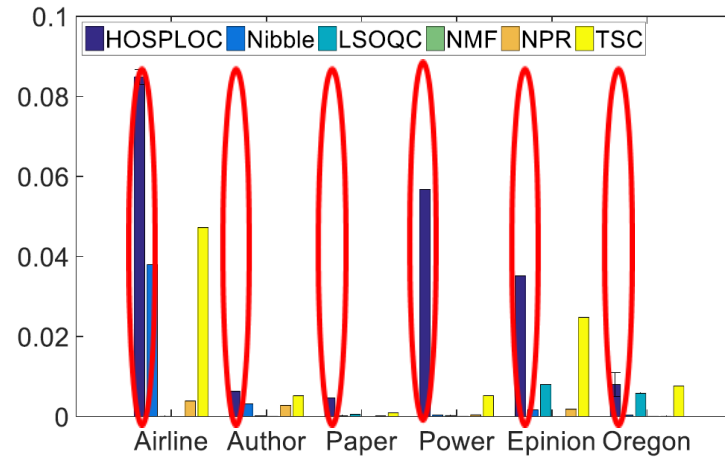


(b) $\Phi(C, triangle)$

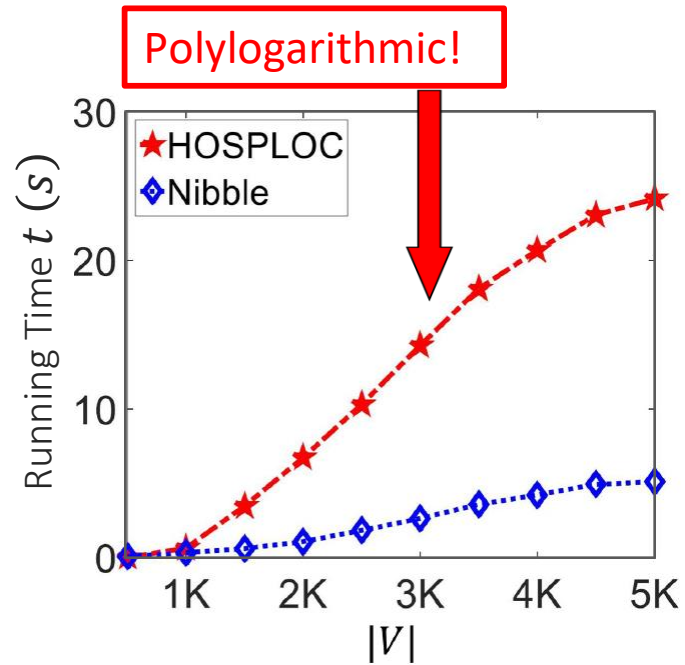


Better
↑
Worse

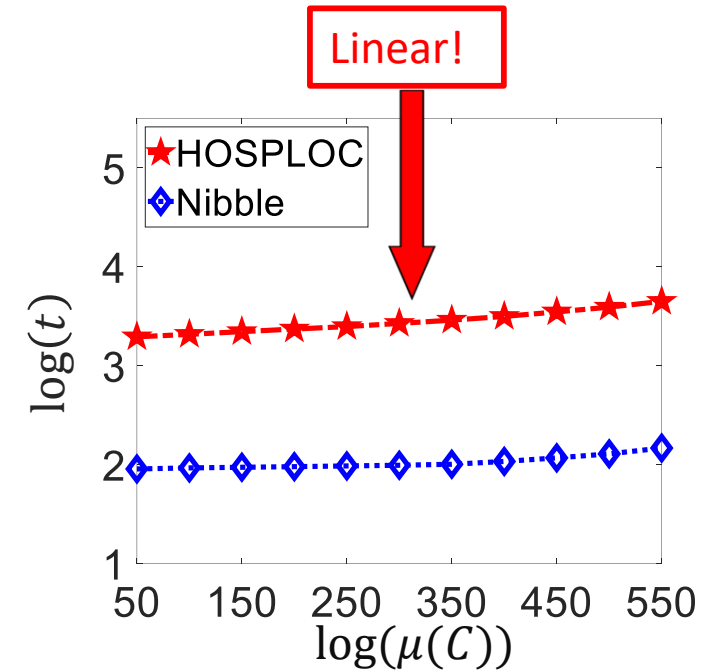
(c) Triangle Density



Scalability Analysis



(a) The number of vertices
V.S running time t



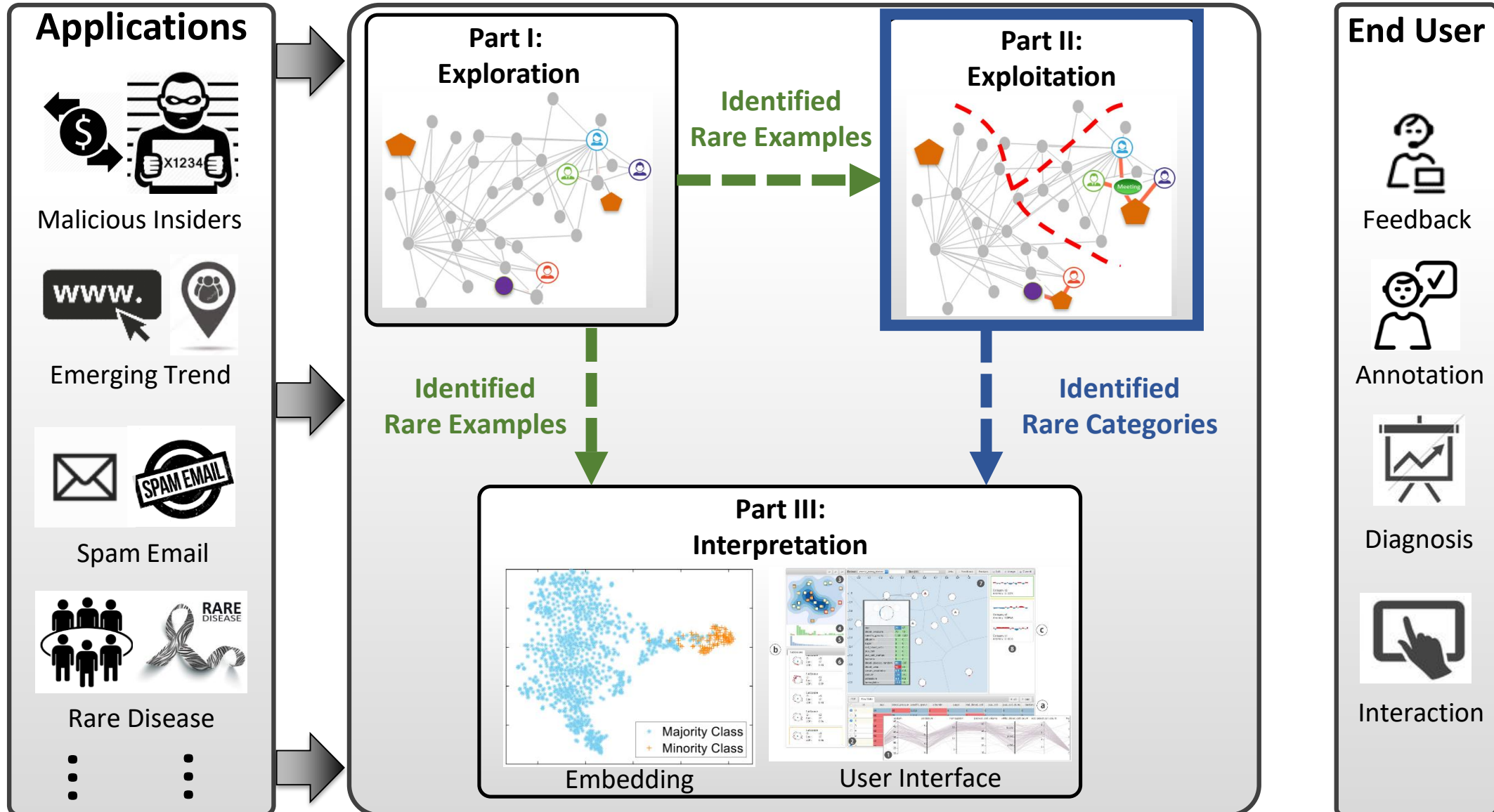
(b) The lower bound of $\log(\mu(C))$
V.S $\log(t)$

* Nibble = A special case of HOSPLOC



Part III:
Rare Category Representation

Overview of Complex Rare Category Analysis



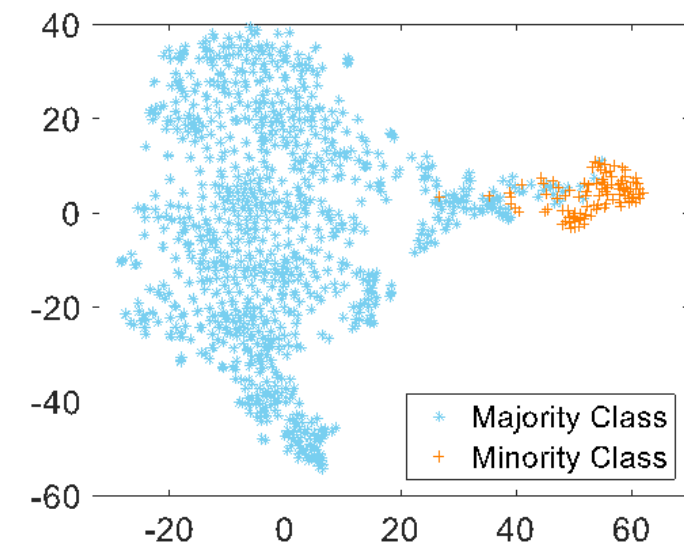
Rare Category Oriented Network Embedding

- Specific Problem Definition

- Given: An attributed network $G = (V, E, X)$, one-shot or few-shot labeled rare examples $L = \{x_1, \dots, x_L\}$, and the desired embedding dimension d .
- Find: A rare category oriented network embedding $E \in R^{n \times d}$, and a list of predicted rare category examples.

- Challenges

- C1: Rarity
- C2: Sparsity of labeled examples
- C3: Non-separability of rare example from the majority classes



Network Layout of Pubmed

Rare Category Characterization (RCC)

- Cost-sensitive Learning (**Address C1**)
 - Focus on rare category examples
 - Learn from the highly-skewed distribution

$$L_S = \sum_{l=1}^L c_{y_l, \hat{y}_l} \log \Pr(\hat{y}_l = 1 - y_l | x_l, e_l)$$

Penalize the error of classify minority class examples into majority classes

- Self-paced Learning (**Address C2**)
 - Start from a handful labeled example
 - Gradually explore more via label propagation

$$L_{RCC} = L_S - \sum_{i=1}^{L+U} v_i^{(1)} \log \Pr(\hat{y}_i = 1 | x_i, e_i) - \sum_{i=1}^{L+U} \lambda^{(1)} v_i^{(1)}$$

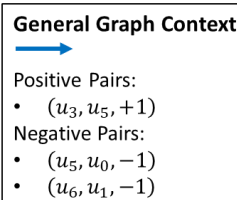
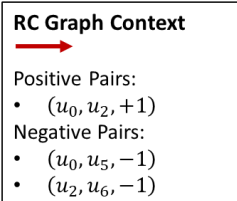
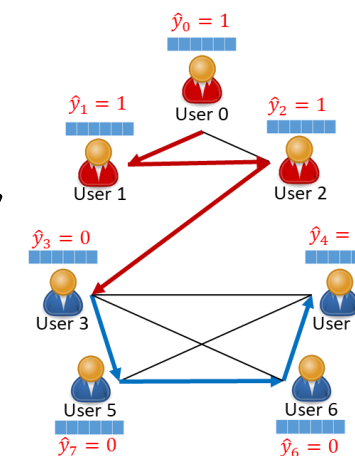
↑ Self-paced Vector
↑ Self-paced Regularizers

Rare Category Embedding (RCE)

- Minimize the cross-entropy loss of predicting context pairs (i, c)

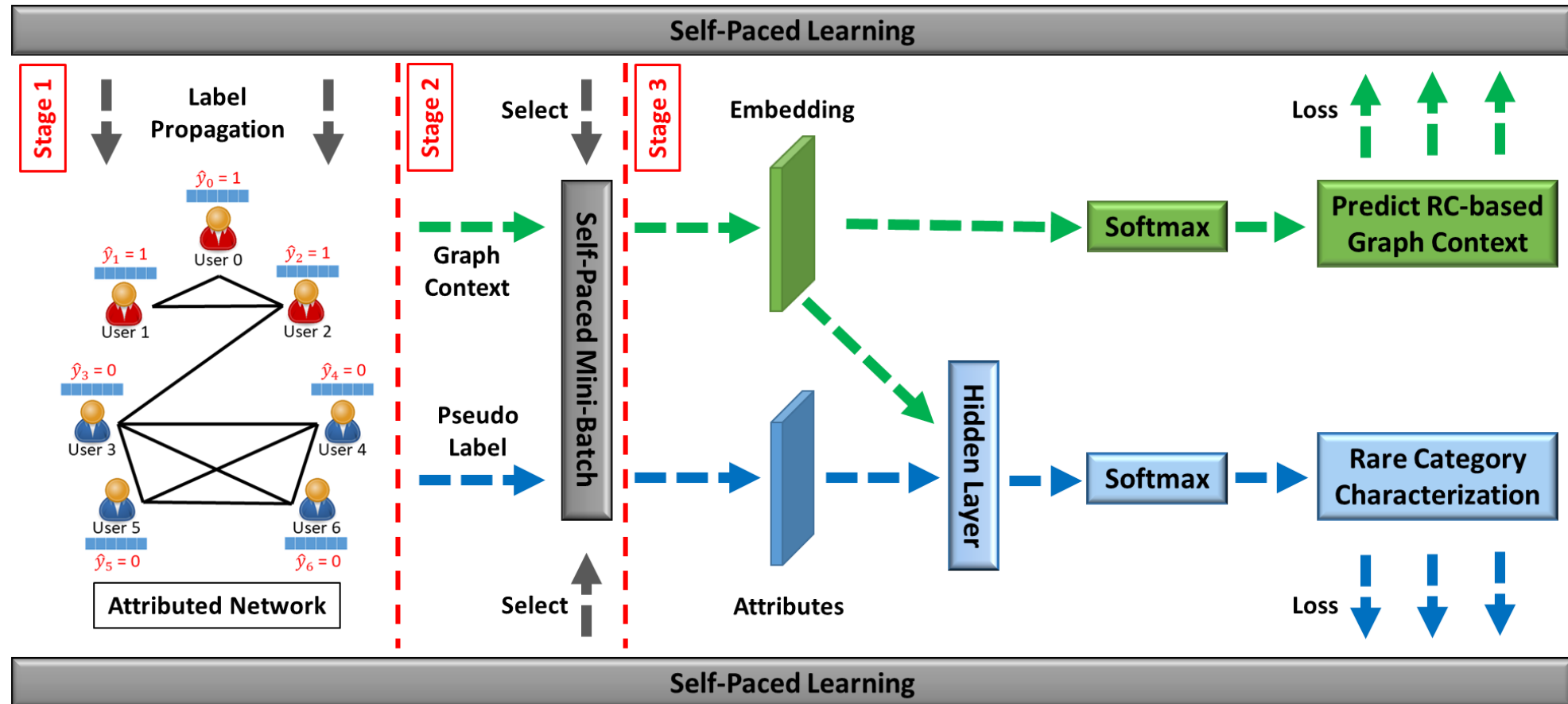
$$\min -E_{(i, c, \gamma)} \log \sigma(\gamma \theta_c^T e_i)$$

- Rare category oriented context sampling (**Address C3**)
 - Indicator vector I from RCC.
 - With probability p , extract general network context.
 - With probability $1 - p$, extract rare category oriented network context starting from the non-zero elements in I .

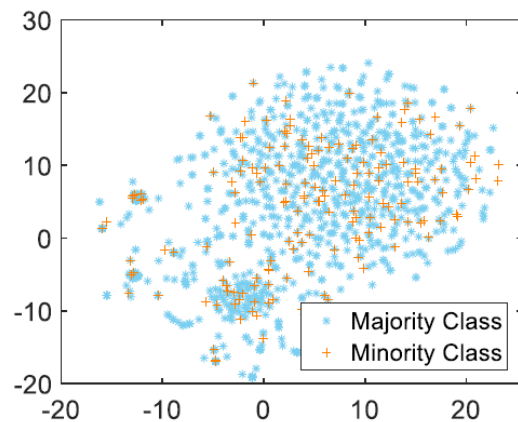


SPARC Algorithm

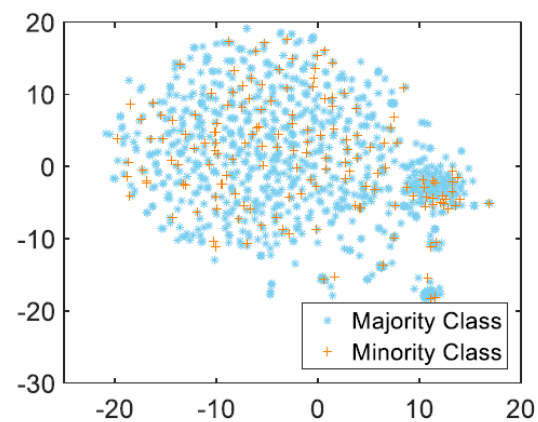
Proposed Framework



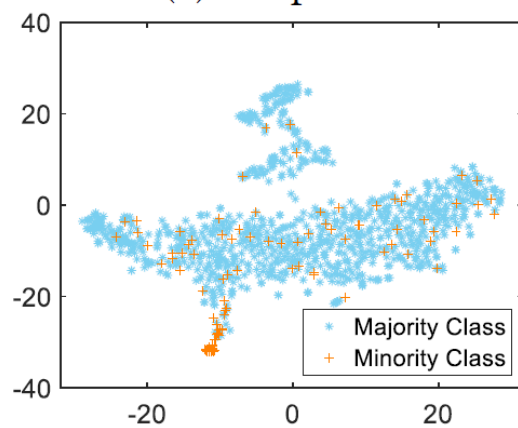
2-D t-SNE Visualization



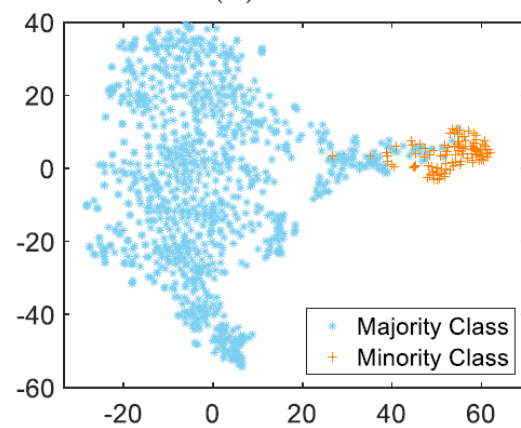
(a) DeepWalk



(b) LINE



(c) PLANETOID



(d) SPARC

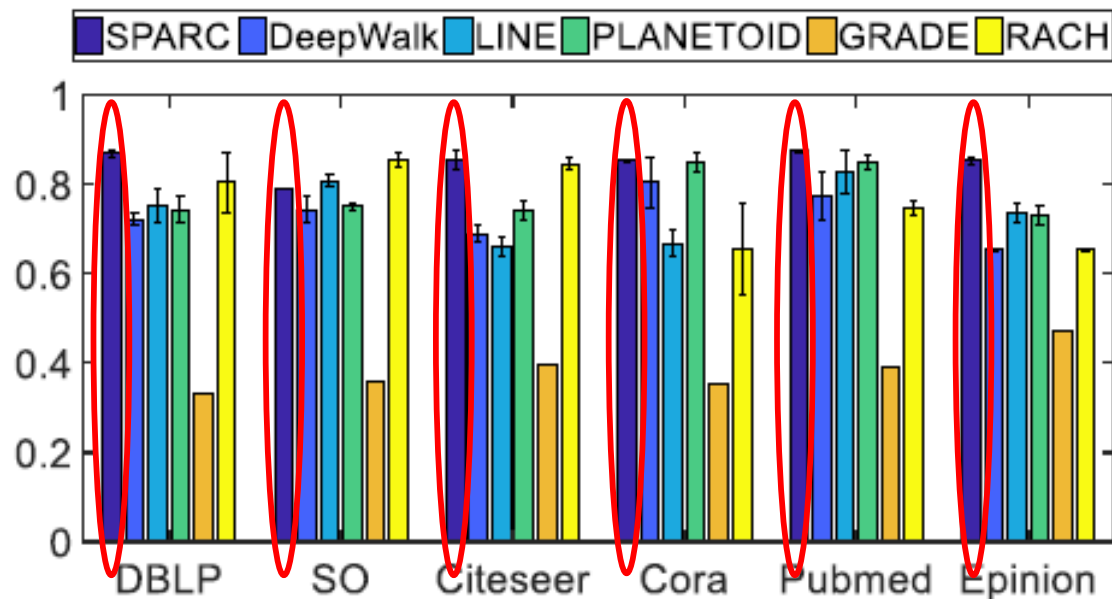
Experimental Results

- Datasets

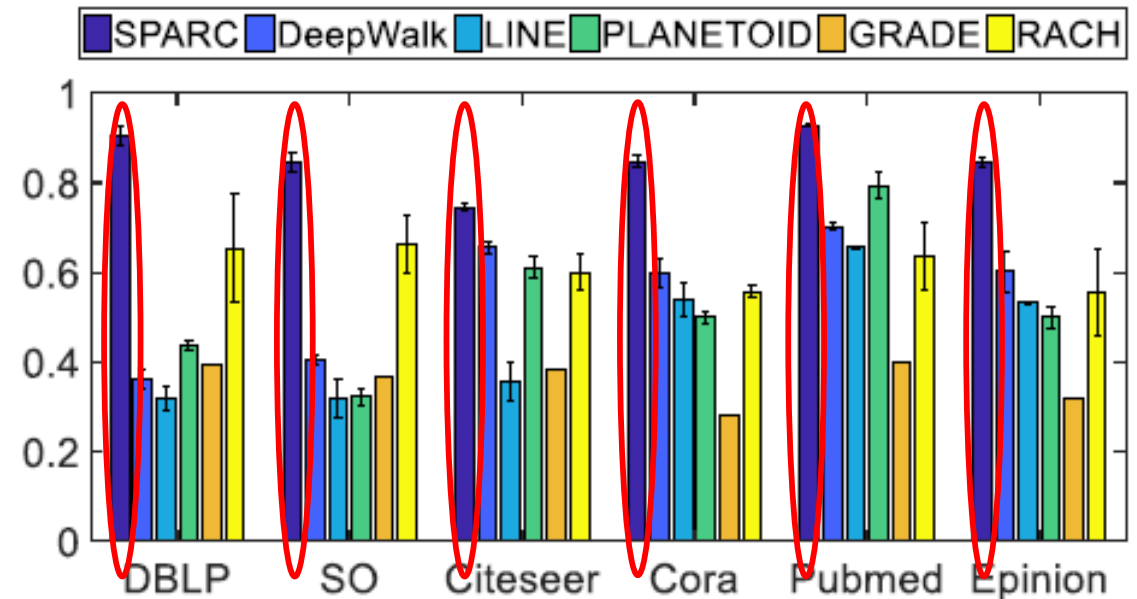
Category	Network	Classes	Smallest Class	Nodes	Edges
Collaboration	DBLP	20	1.91%	2,309	7,913
	SO	2	1.29%	3,262	19,926
NLP	Citeseer	6	3.42%	3,327	4,732
	Cora	7	1.14%	2,708	5,429
	Pubmed	3	4.05%	19,717	44,318
Social	Epinion	19	1.38%	75,879	508,837

Experimental Results

- Effectiveness analysis with 5% labeled minority class examples.



(a) Accuracy

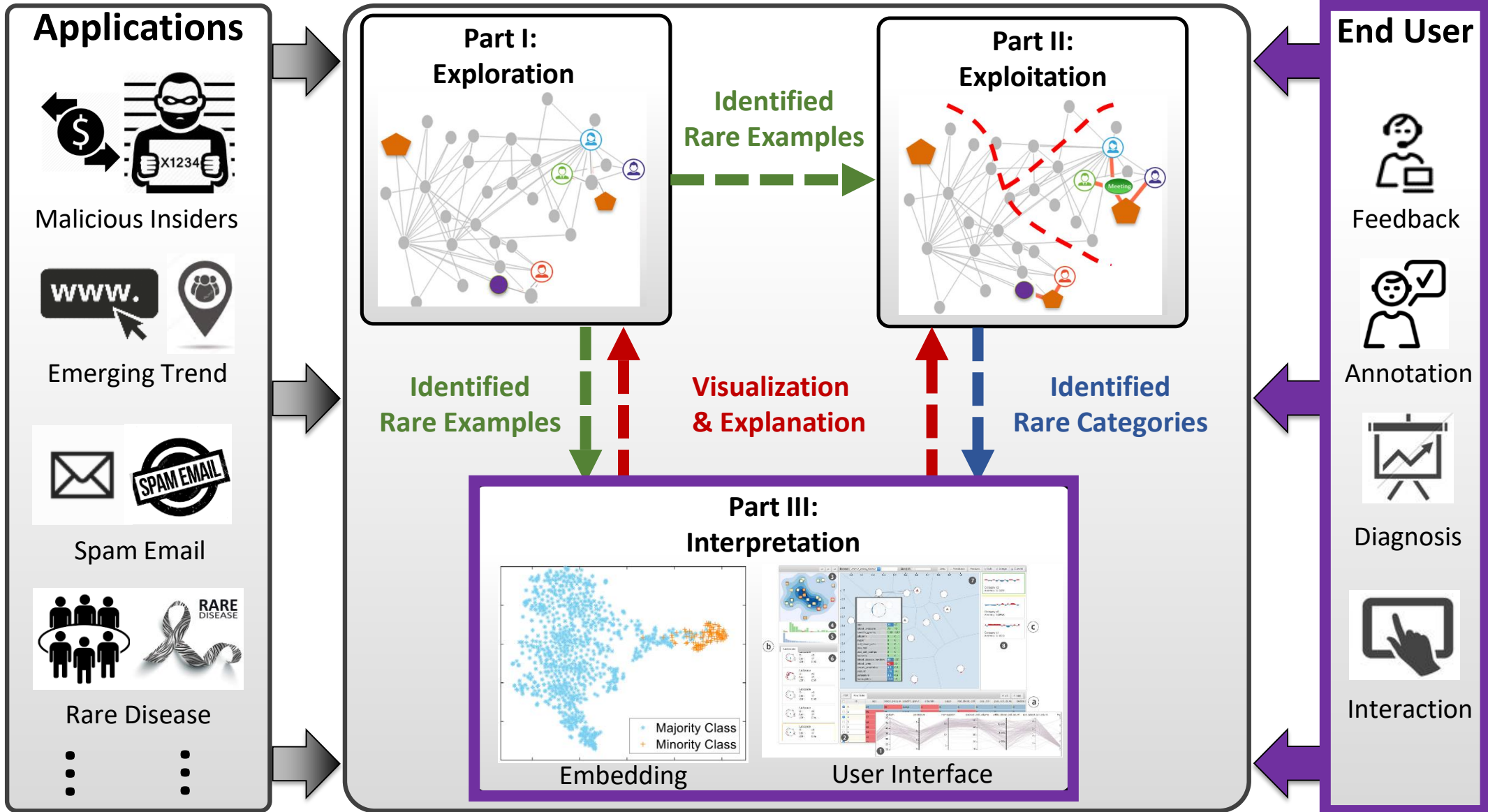


(b) Recall



**Part IV:
Rare Category Analysis
Interpretation**

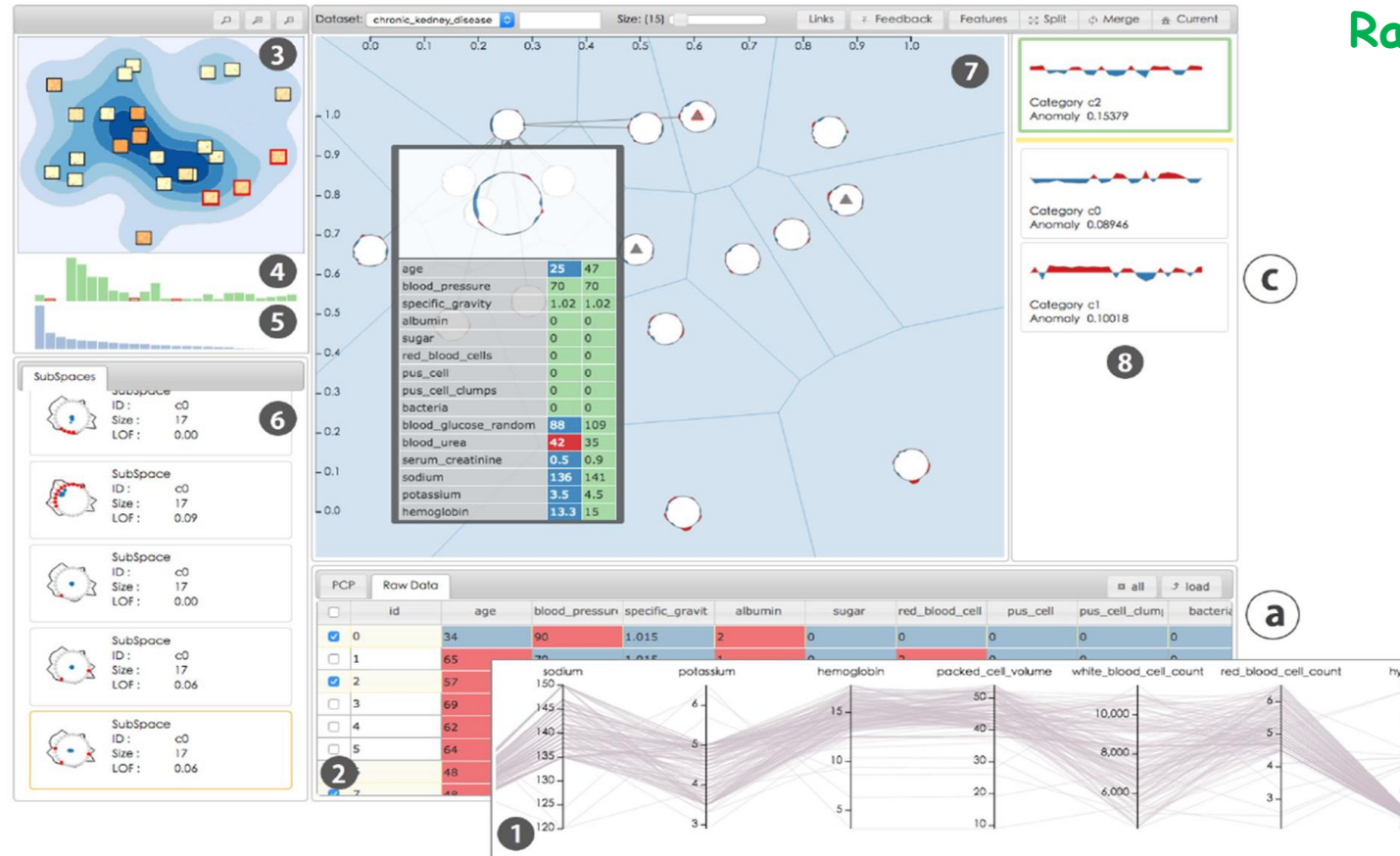
Overview of Complex Rare Category Analysis



The Prototype System

Feature Selection Module

b



Rare Category Analysis Module

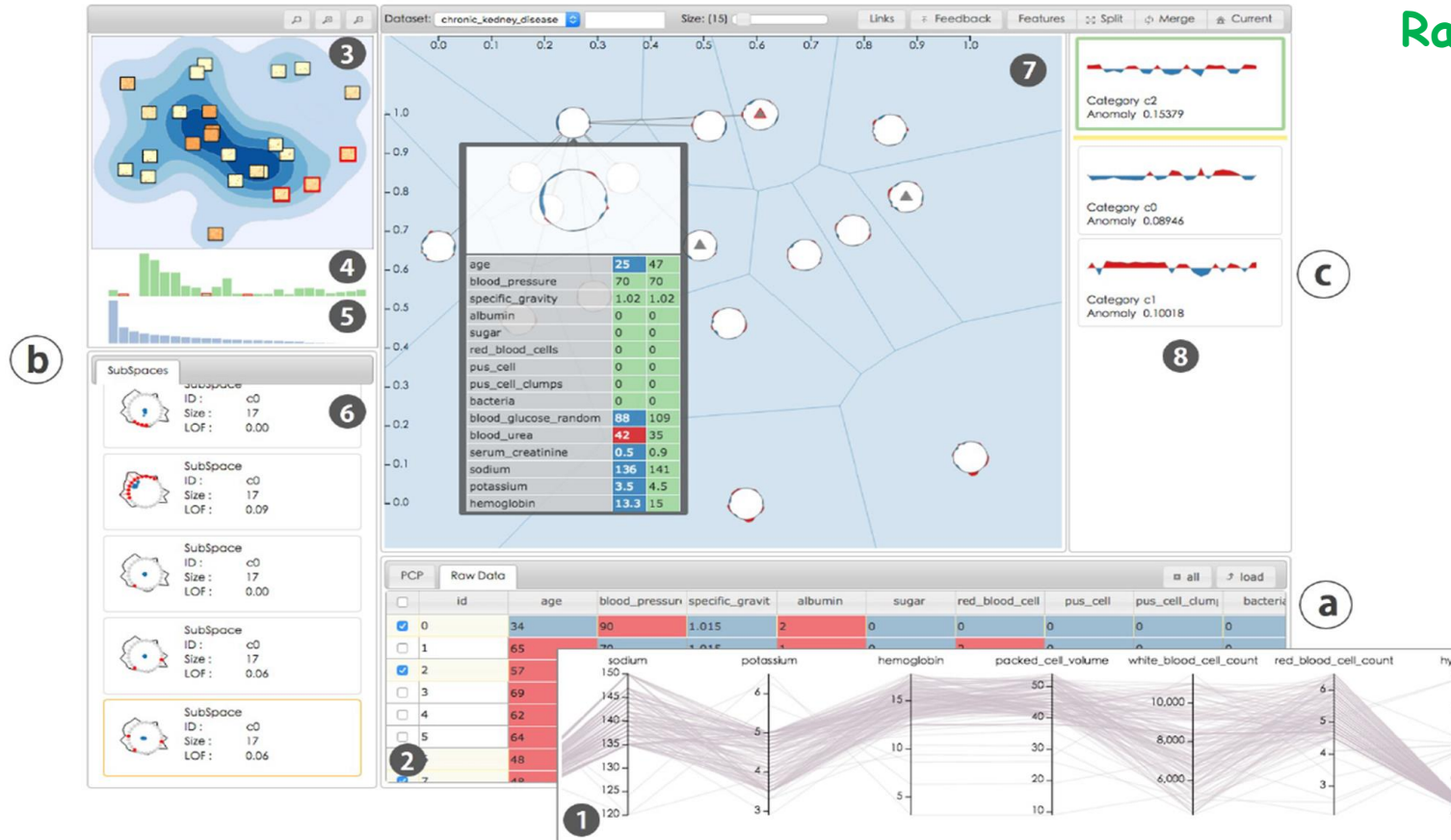
c

Data Exploration Module

a

The Prototype System

Feature Selection Module



Rare Category Analysis Module

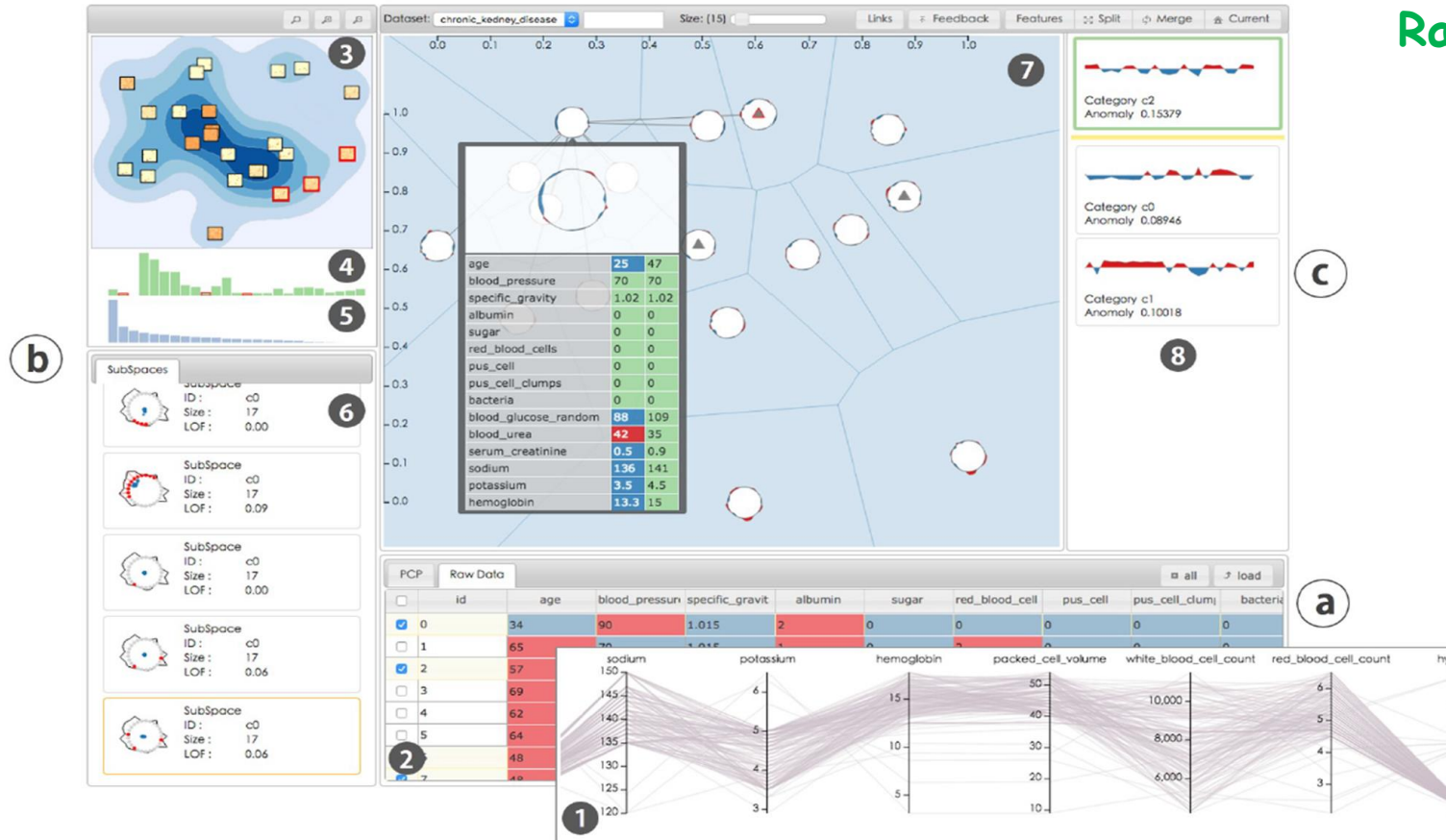
Data Exploration Module

- Represent raw data
- Interactive visualization for data querying
- Support Data filtering

The Prototype System

Feature Selection Module

- Visualize the Variance of data
- Visualize the correlation of data
- Guide the feature selection and subspace investigation process



Rare Category Analysis Module

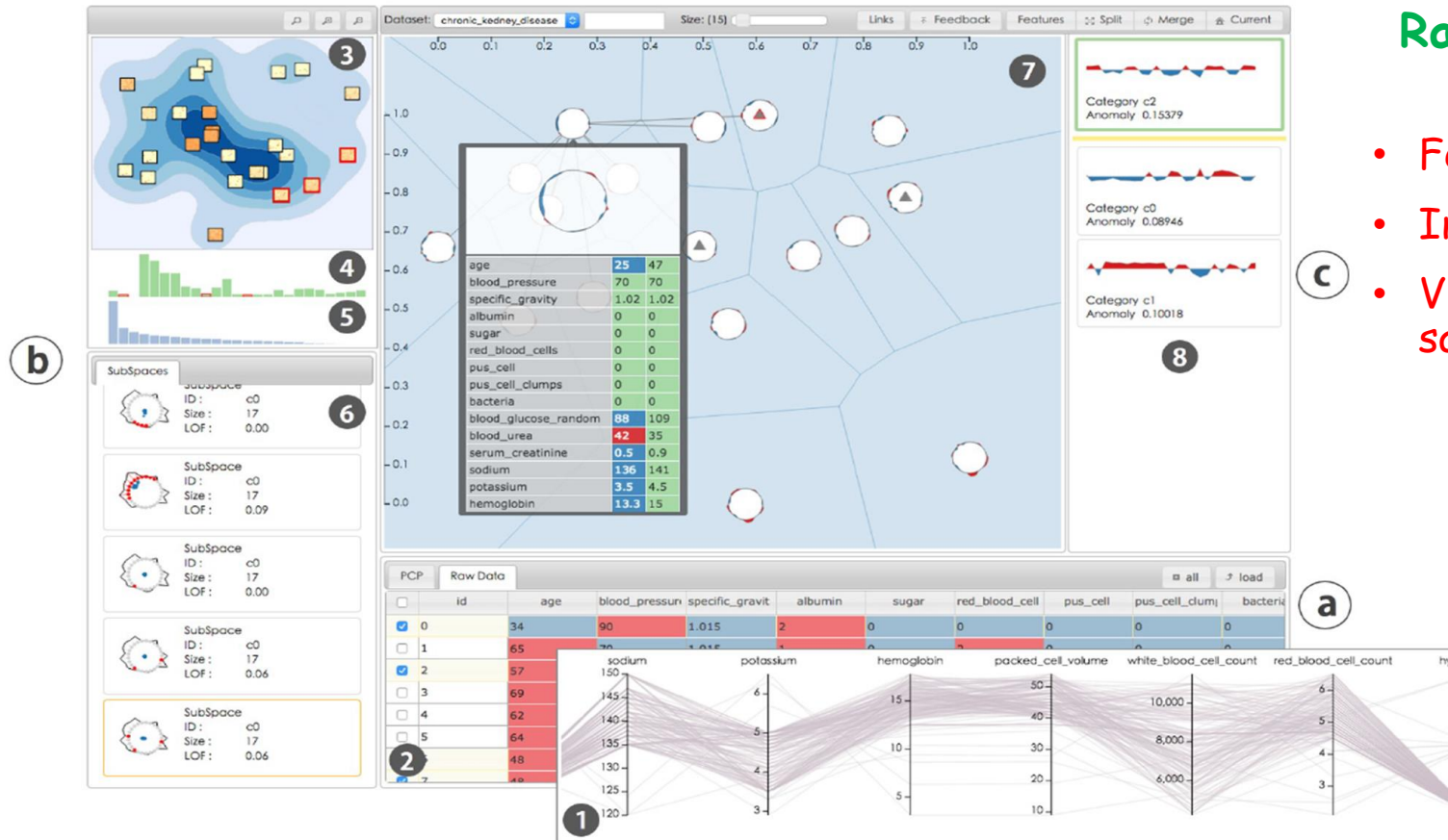
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Rare Category Analysis Module

- Feature selection
- Interactive active learning
- Visualize rare examples in a salient representation

Data Exploration Module

- Represent raw data
- Interactive visualization for data querying
- Support Data filtering

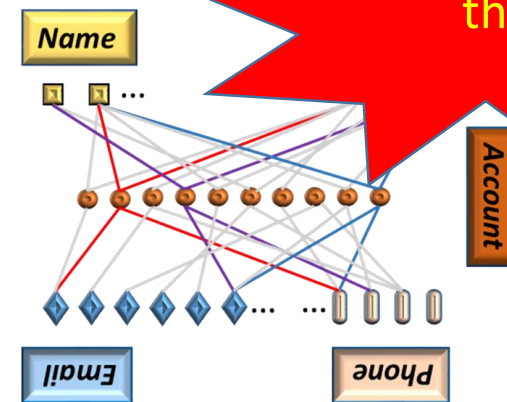
A Case Study in Financial Fraud Detection

- Problem
 - Given: Personal identification information (PII) network of the bank customers.
 - Find: Suspicious synthetic identities.

- Identified Abnormal Patterns



PII Network



Identified Rare Category



**Part IV:
Challenges & Future Directions**

Next Generation Rare Category Analysis System

- Built Upon Four Key Pillars

- P1. Comprehension: **Theoretical** foundation of rare category analysis.

- P2. Explainability: **Understandable** rare category prediction models.

- P3. Robustness: **Trustworthy** of RCA models.

- P4. Scalability: **Bounded/Constant** computational complexity.

- Advancing High-Impact Applications

- Aviation Safety

- Healthcare

- Manufacturing

- Finance

- Security

P1. Comprehension

- Observations
 - O1: Different assumptions behind different types of heterogeneity

Heterogeneity	Underlying Assumption
Task	Task Relatedness
View	View Consistency
Instance	Bi-level Label Relationship
Oracle	Better-than-Random

- O2: As the learning model becomes more complex by encoding more types of heterogeneity in the rare category analysis models
 - The likelihood of model assumption **violation** increases
 - The likelihood of model **over-fitting** increases

P2. Explainability

$$\varepsilon(x) = \operatorname{argmin}_{g \in G} \mathcal{L}(f, g, \pi_x) + \Omega(g)$$

$\mathcal{L}(f, g, \pi_x)$

- f : rare category analysis model
- π_x : Local vicinity of example x
- L : Model fidelity function

$\Omega(g)$

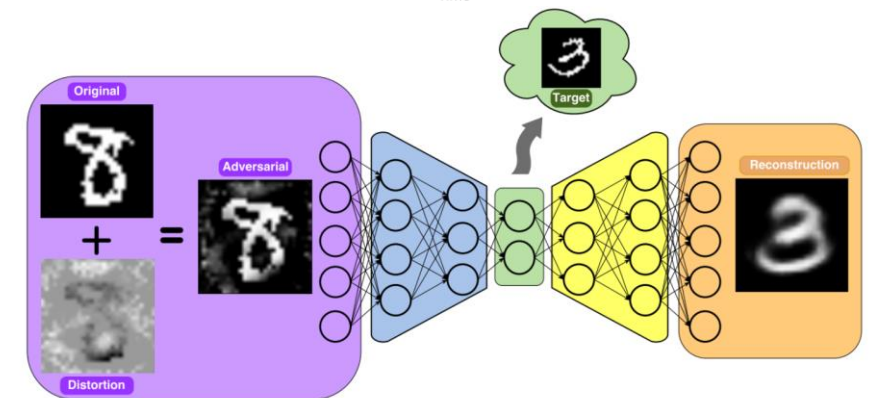
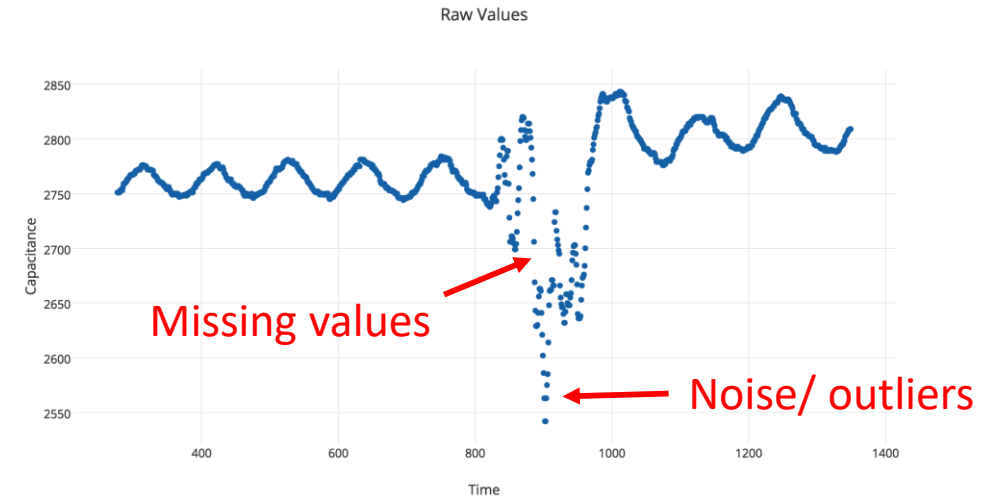
- $g \in G$: Interpretable model
- $\Omega(g)$: Model complexity (*inversely proportional* to model interpretability)

	Problem	State-of-the-art	Future Directions
Fidelity	Supervision	Output of outlier detection model	<ul style="list-style-type: none"> • Query values; • Correct wrong predictions
	Model Types	Flat models	<ul style="list-style-type: none"> • Hierarchical • Multi-resolution
Explainability	Data Sensitivity	NA	<ul style="list-style-type: none"> • Relevant instances • Relevant features
	Model Diagnosis	NA	<ul style="list-style-type: none"> • Explaining correct or wrong predictions
	Model Improvement	NA	<ul style="list-style-type: none"> • Explainable “user in the loop” learning process

Key Insight: Data heterogeneity brings both challenges and opportunities for explainability!

P3. Robustness

- Operational Robustness
 - Ex. Noise, outliers, missing values
- Adversarial Robustness
 - Ex. Adversarial attacks



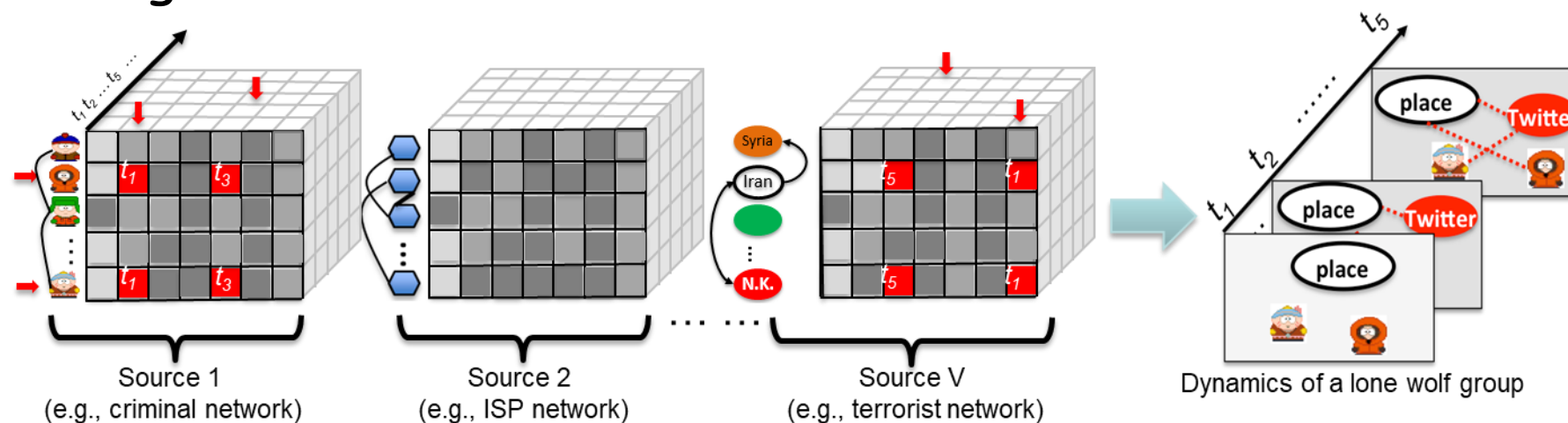
[Tabacof et al., NIPS 2016]

Two competing hypotheses for robust learning in the presence of data heterogeneity

- H1: Heterogeneity makes the learning system more vulnerable (more attacking channels for adversaries, possibly causing **a cascading attack**).
- H2: Heterogeneity makes the learning system more robust (it makes the attacker harder to generate examples that is **universally adversarial**, i.e., it becomes harder to fool ALL the learning tasks).

P4. Scalability

- Key Research Questions
 - Time Complexity
 - Space Complexity
- A Case Study: Long-Wolf Attack Detection
 - Multi-Sourced Data
 - Evolving over time



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